





Layered Drawing of Undirected Graphs with Generalized Port Constraints

Julian Walter, **Johannes Zink**, Joachim Baumeister, Alexander Wolff

• Imagine you own a machine manufacturing company.

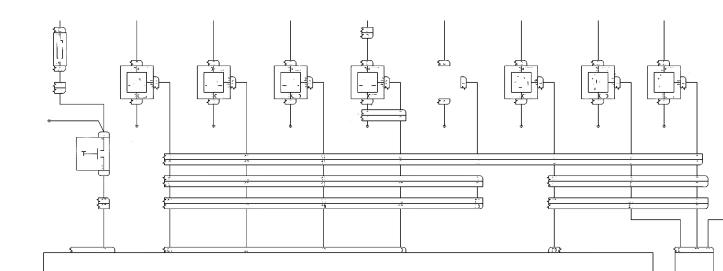
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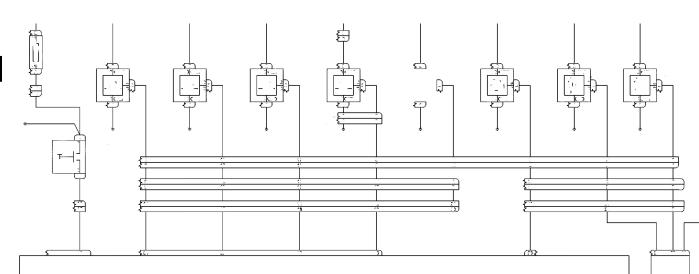
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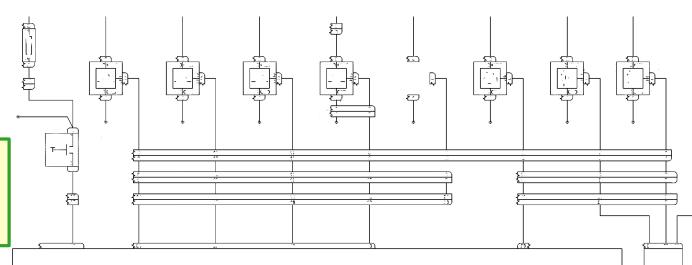


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 - orthogonal style
 - vertices arranged on few layers



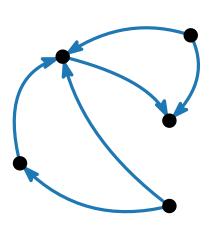
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⇒ use layered graph drawing algorithm

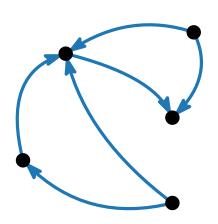


• Given: directed acyclic graph G = (V, A)

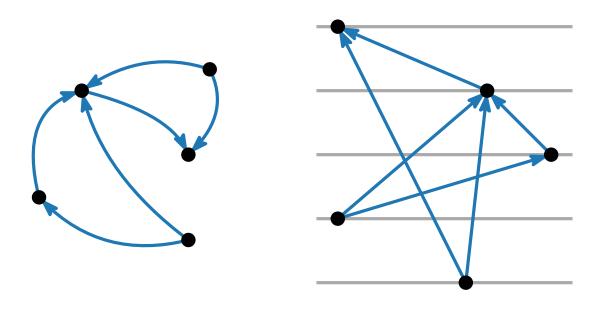
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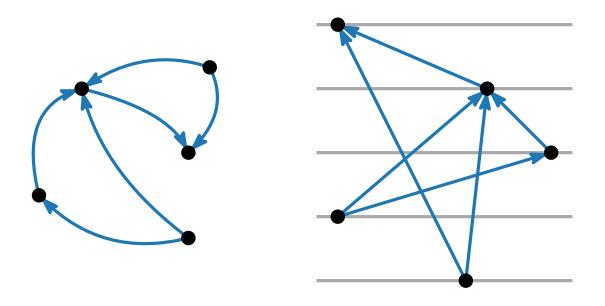
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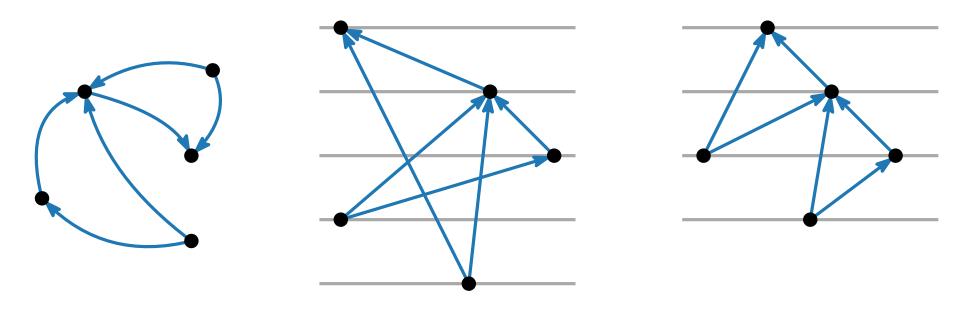


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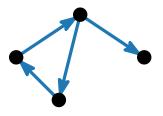


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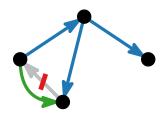
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Consists of 5 phases:

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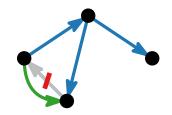


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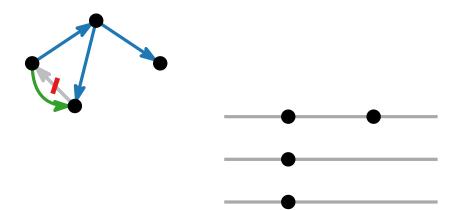
1. cycle elimination



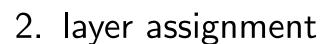
2. layer assignment

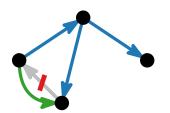
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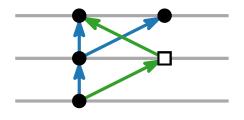




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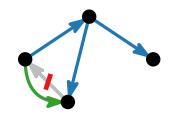




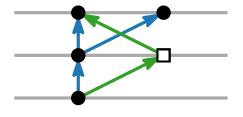


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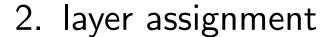


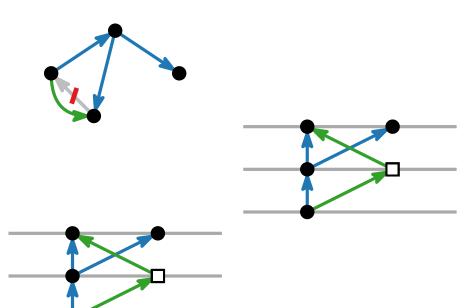
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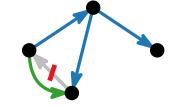
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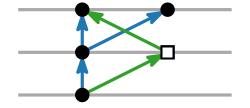


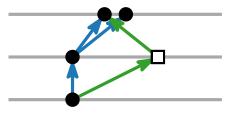
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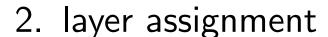
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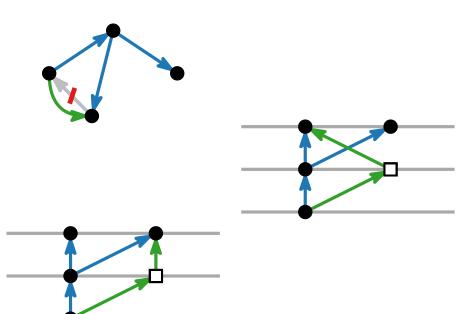




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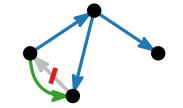
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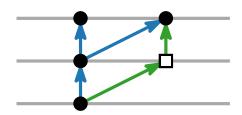


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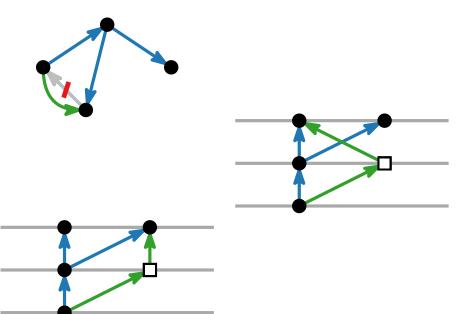


- 2. layer assignment
- 3. crossing minimization

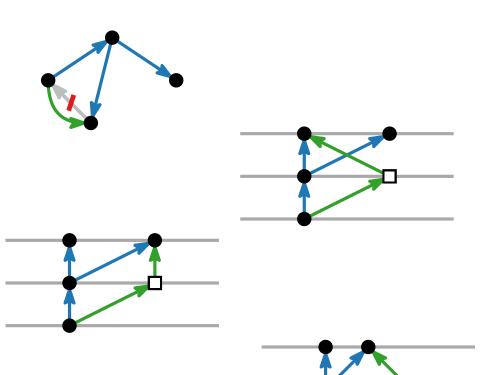


4. node placement

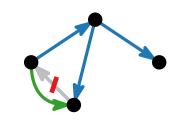
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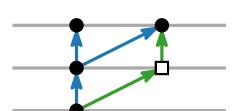


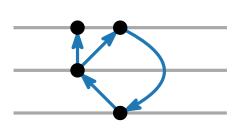
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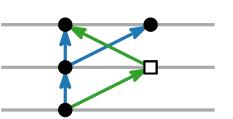


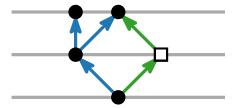
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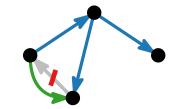




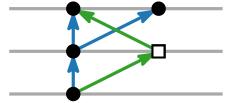


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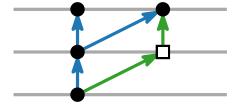
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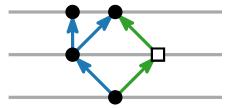
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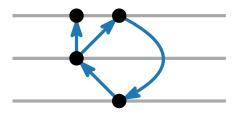
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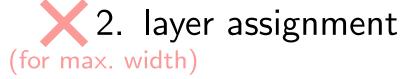
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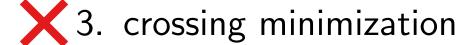


contains NP-hard tasks

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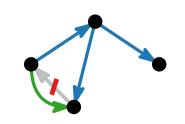


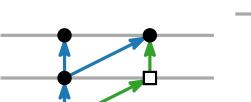


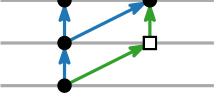


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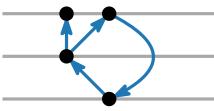
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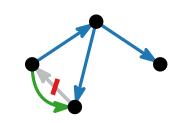


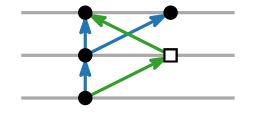


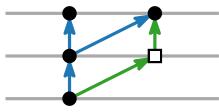
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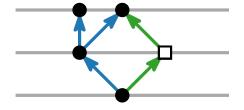
- 1. cycle elimination
- 2. layer assignment (for max. width)
 - **X** 3. crossing minimization
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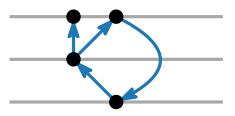
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⇒ use heuristics

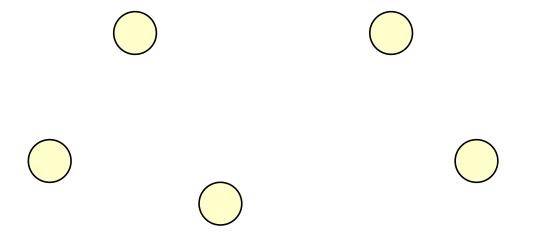
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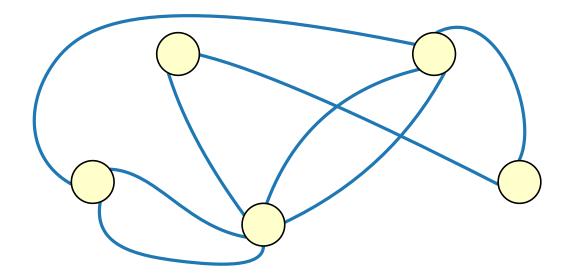
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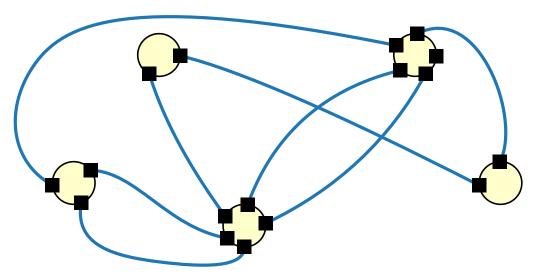
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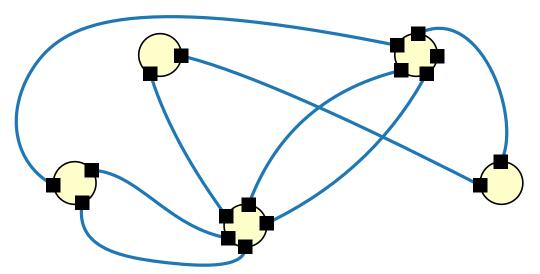
Extension of a graph to a port graph G = (V, P, E):

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- port set P s.t. each $p \in P$ belongs to some $v \in V$



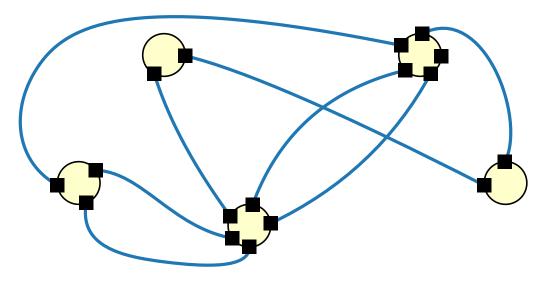
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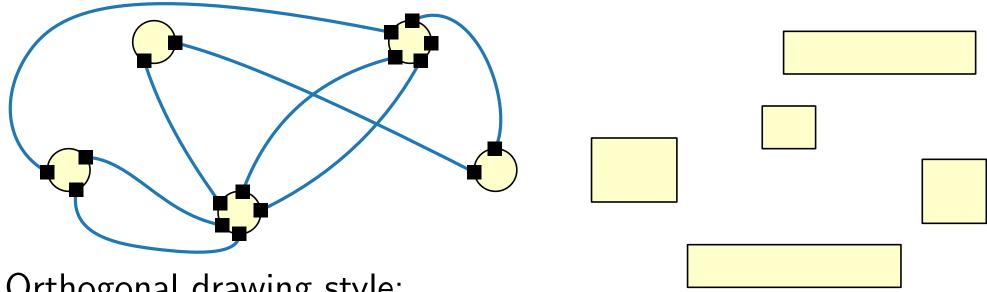
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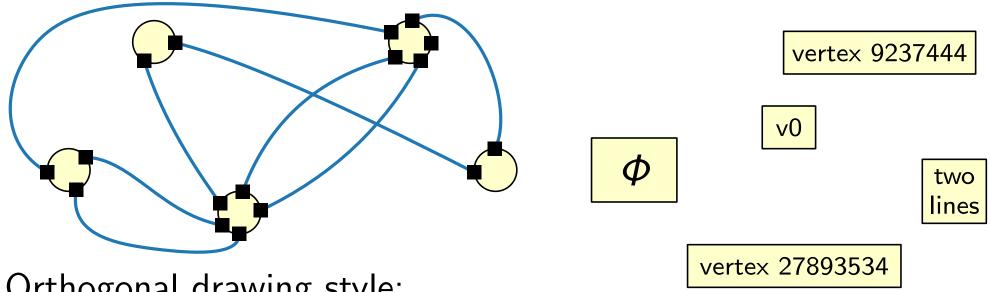


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• $v \in V$: axis-aligned rectangle of width $\geq w(v)$, height $\geq h(v)$

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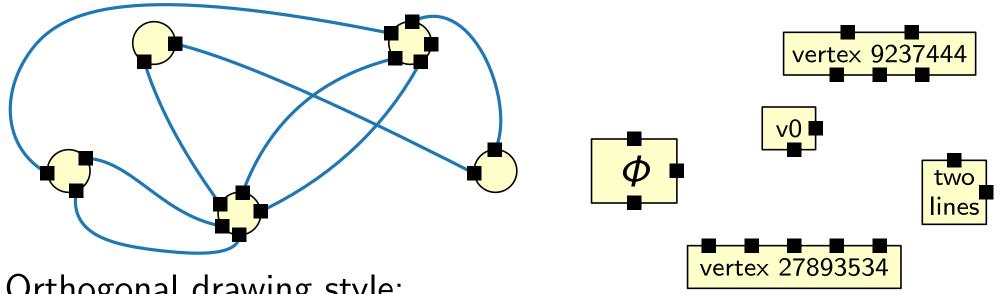


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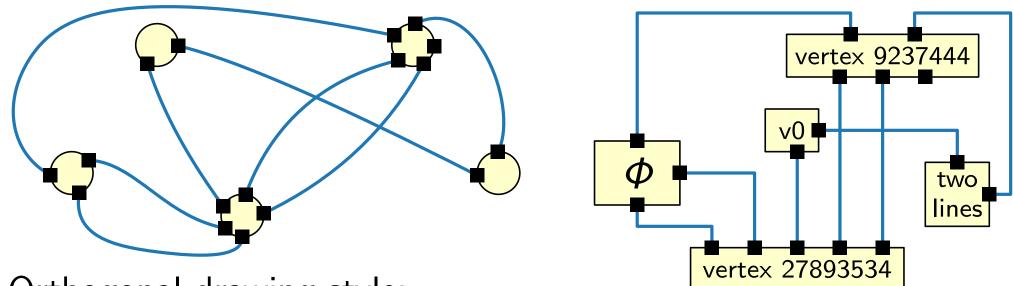


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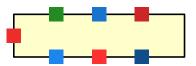
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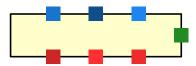
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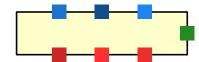
- FIXEDSIDE



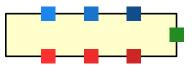
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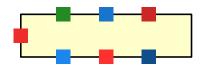
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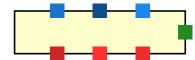
- FIXEDORDER



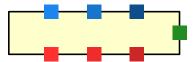
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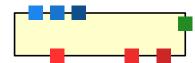
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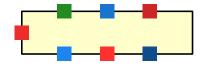
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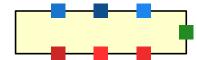
- FixedPos



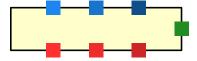
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 - Free



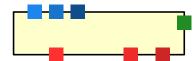
- FIXEDSIDE



- FIXEDORDER



- FixedPos



 Open source implemenation in Java as KIELER (later: eclipse.elk) available

We extend an orthogonal-style layered graph drawing algorithm built on the Sugiyama framework with ports by:

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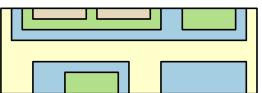
We extend an orthogonal-style layered graph drawing algorithm built on the Sugiyama framework with ports by:

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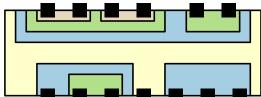
- can be assigned to a vertex side or FREE

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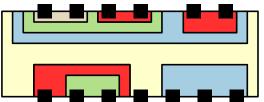
- can be assigned to a vertex side or FREE
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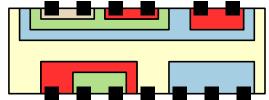
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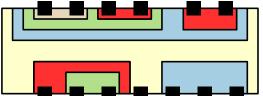
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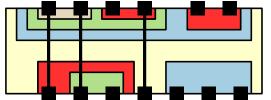
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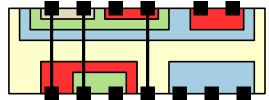


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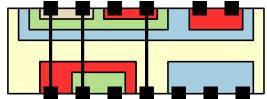
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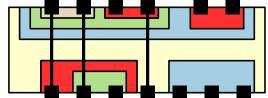
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Draw undirected graphs by orienting the edges using



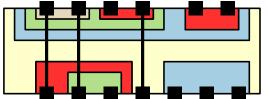
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 - breadth-first search (orient in direction of discovery)



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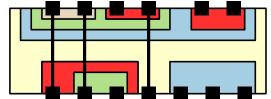


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We experimentally evaluate our variants on real cable plans and pseudo plans (we describe how we generate them from real data)

1. cycle elimination

2. layer assignment

3. crossing minimization

4. node placement

- 1. cycle elimination
- 1. Orient undirected edges (w/o creating cycles)
 - with breadth-first search (BFS)
 - with force-directed algorithm (FD)
 - by random placement (RAND)
- 2. layer assignment

3. crossing minimization

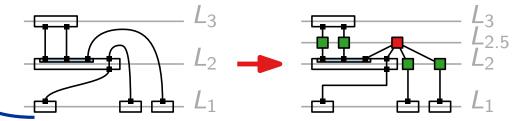
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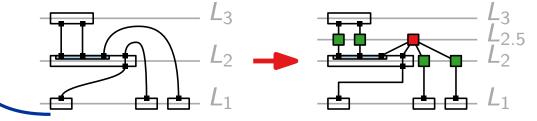
 L_3 L_2 L_1

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- Vertices sort ports afterwards
- PORTS sort port groups & vtcs.
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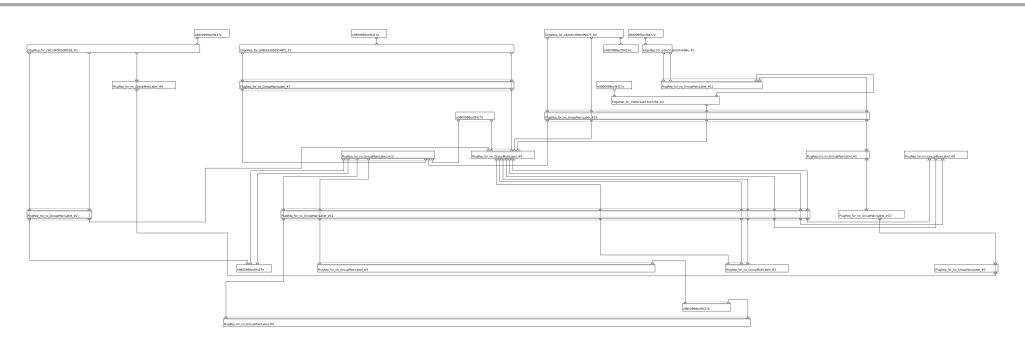
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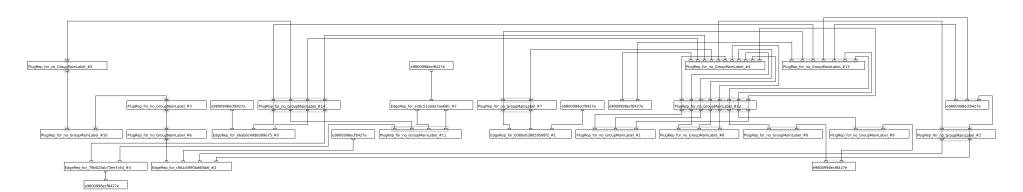
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- Our implementation in Java is available on github: github.com/j-zink-wuerzburg
 - .../praline
 - .../pseudo-praline-plan-generation

Example: (anonymized) plan from REAL

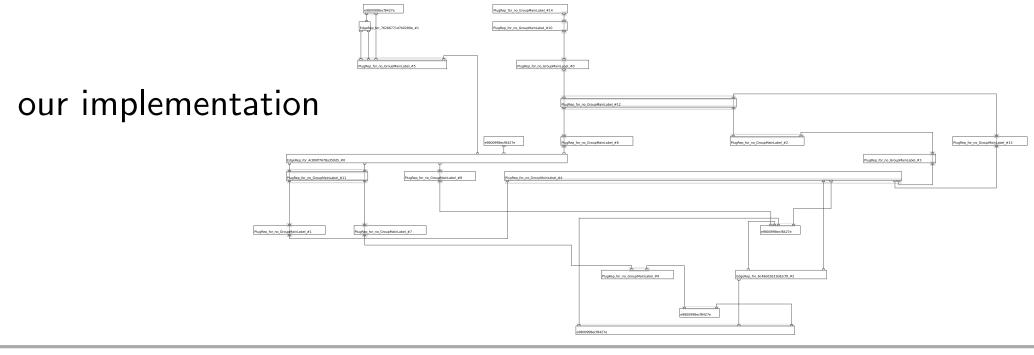


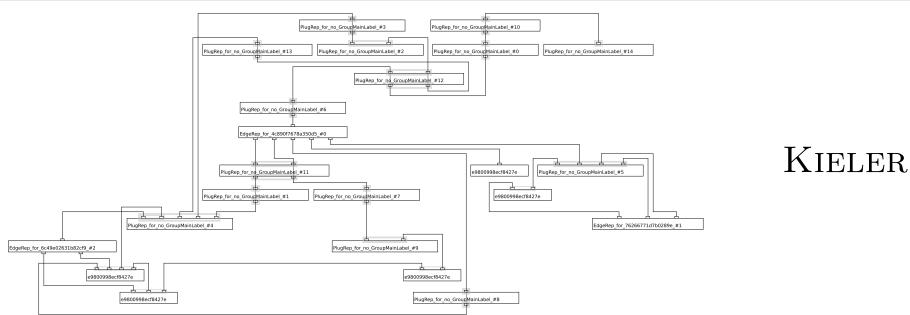
our implementation

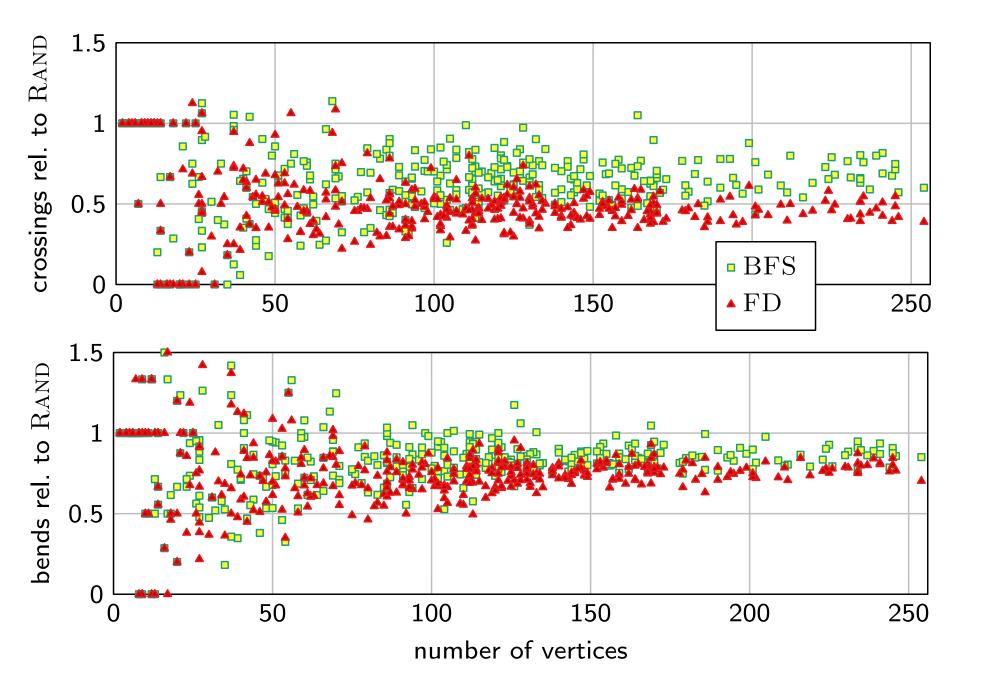


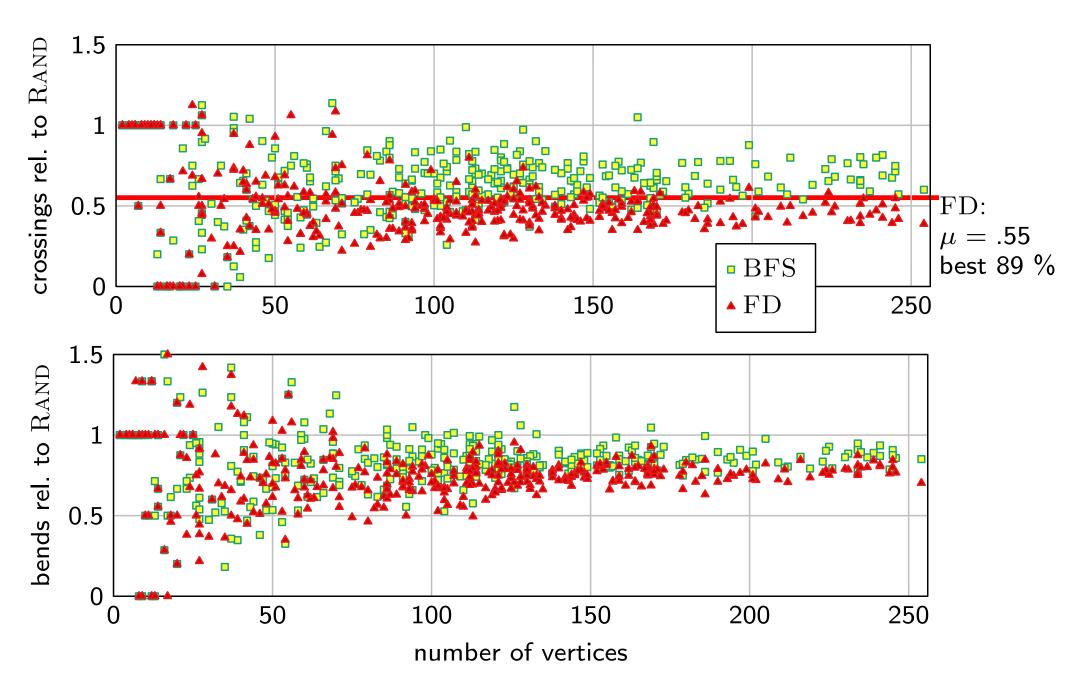
KIELER

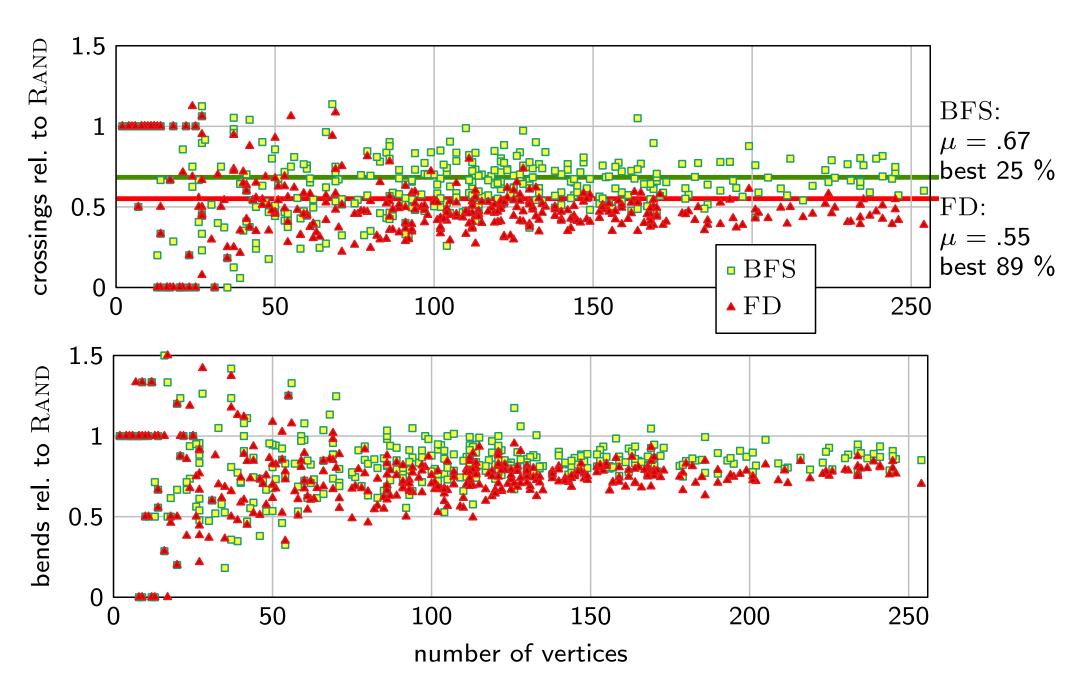
Example: plan from PSEUDO

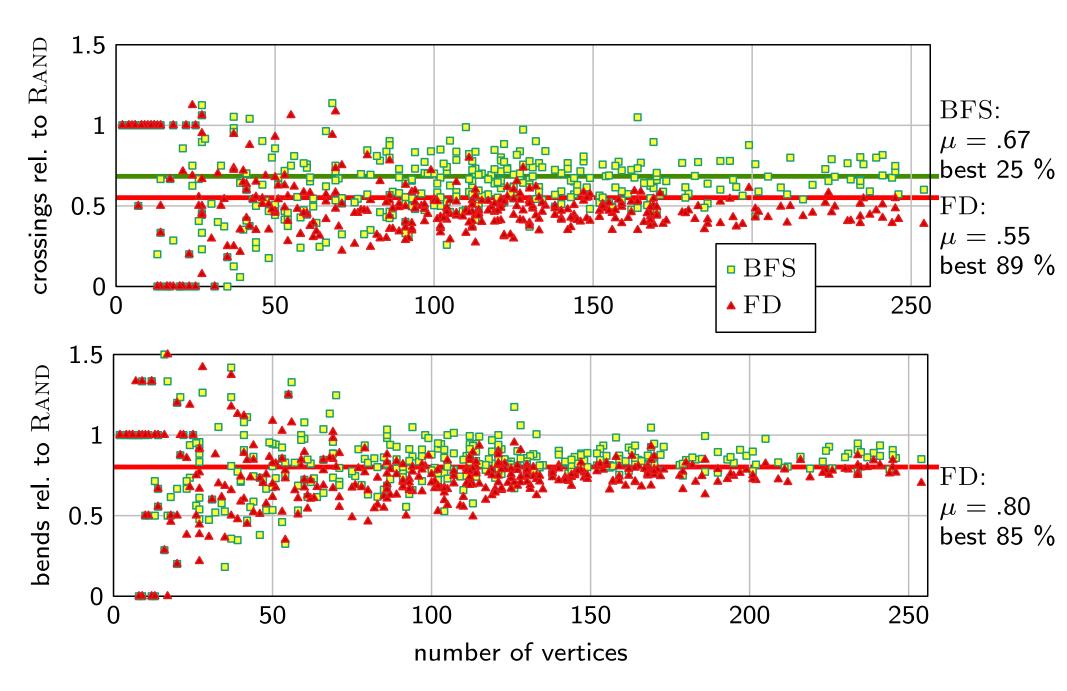


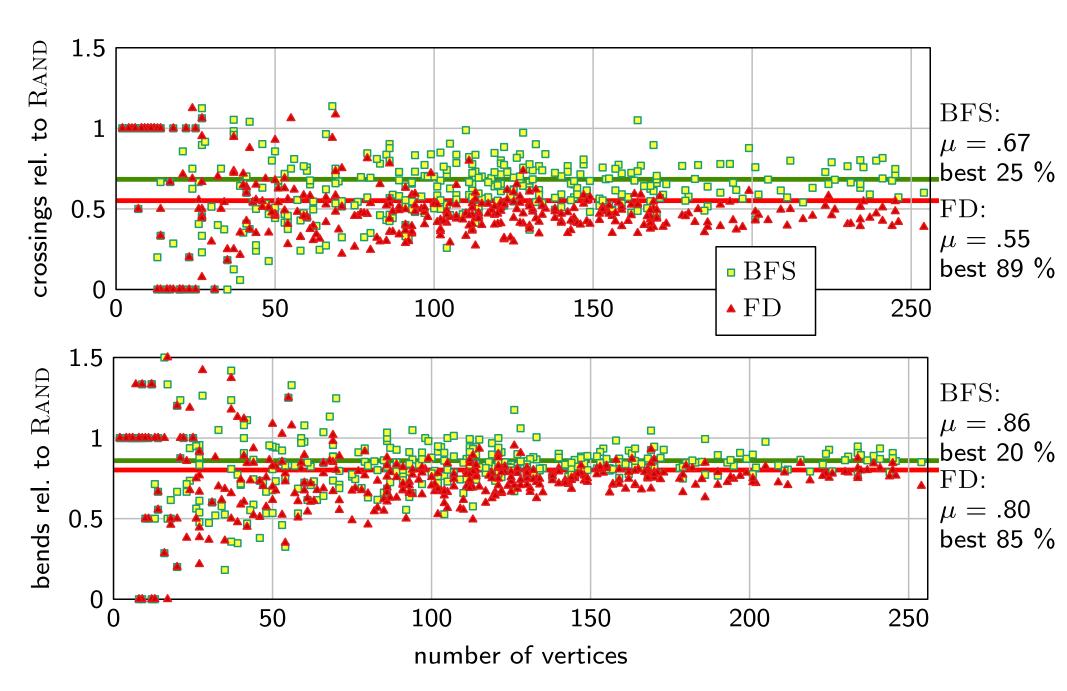




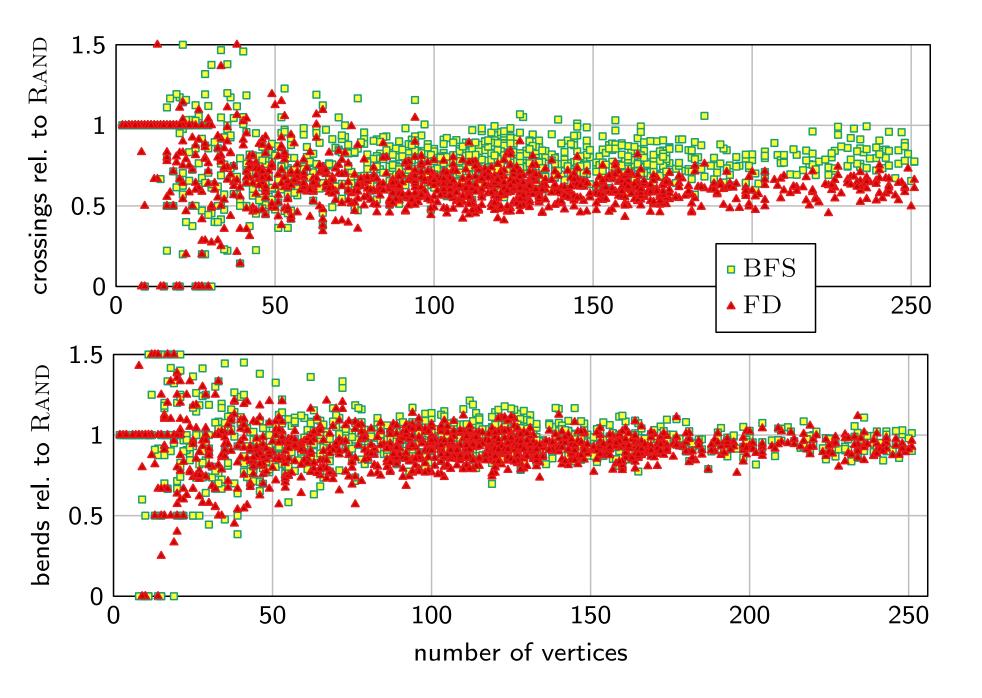




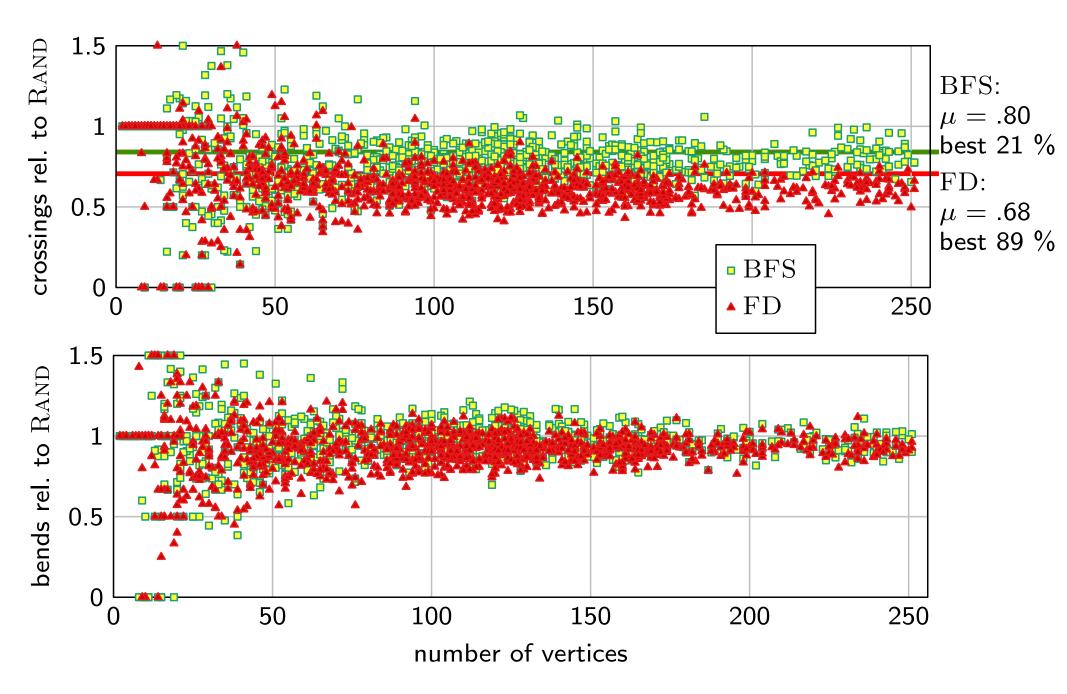




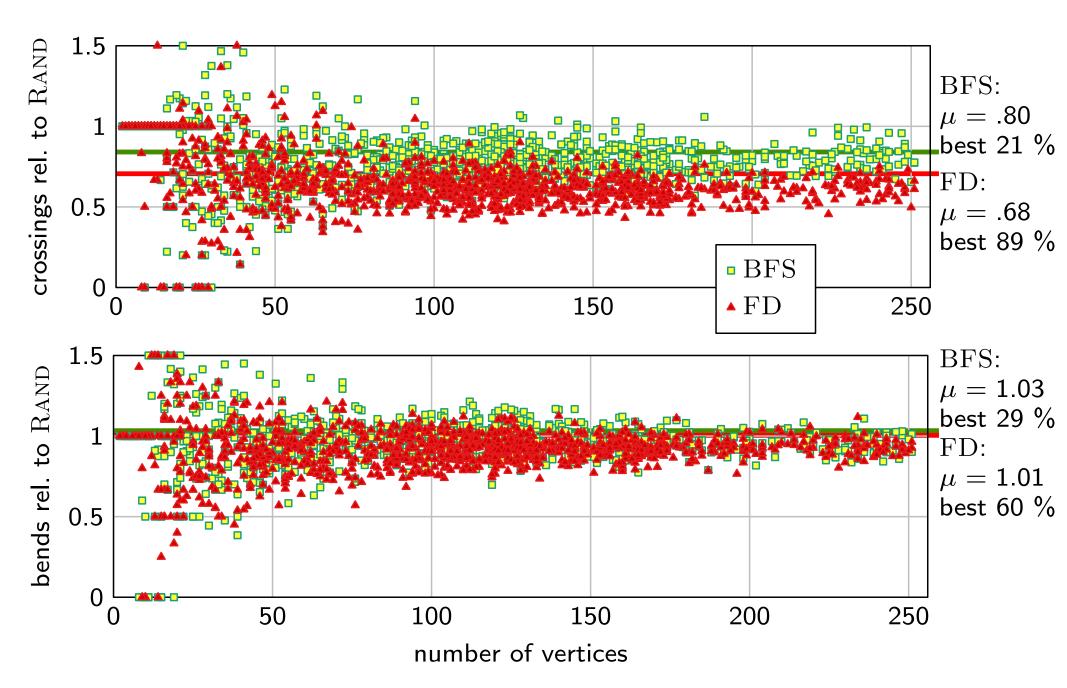
Results: Orienting Edges (PSEUDO)

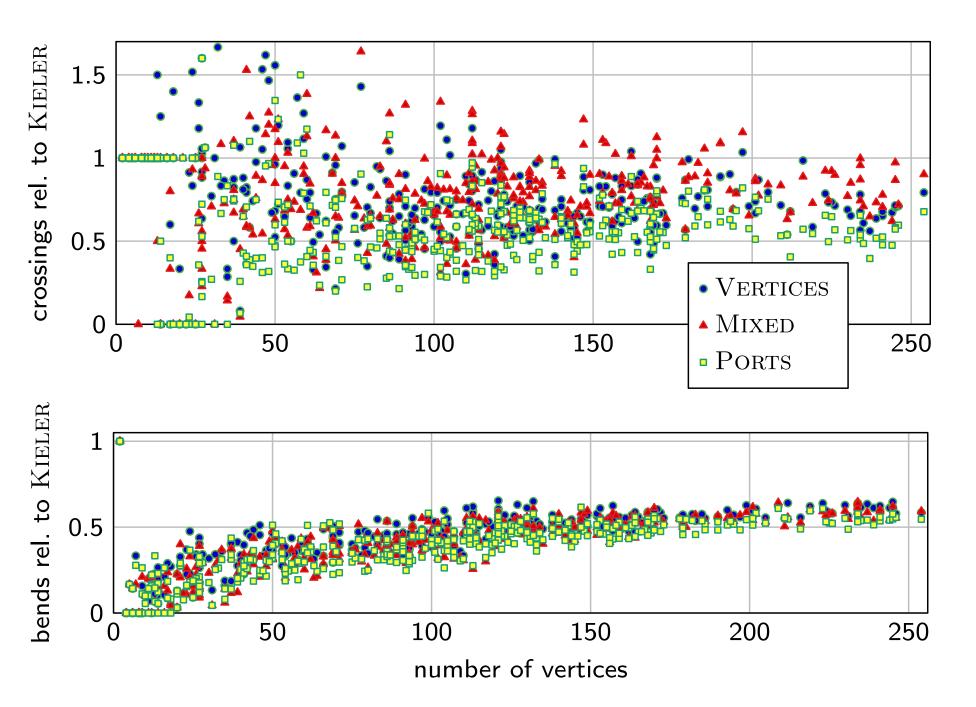


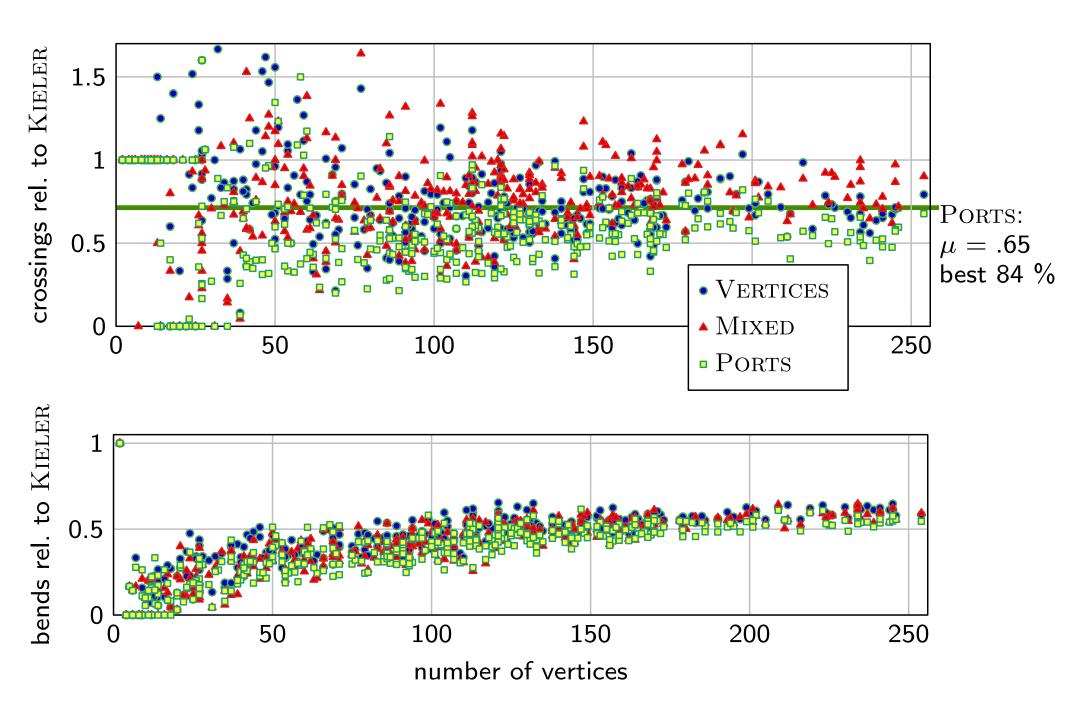
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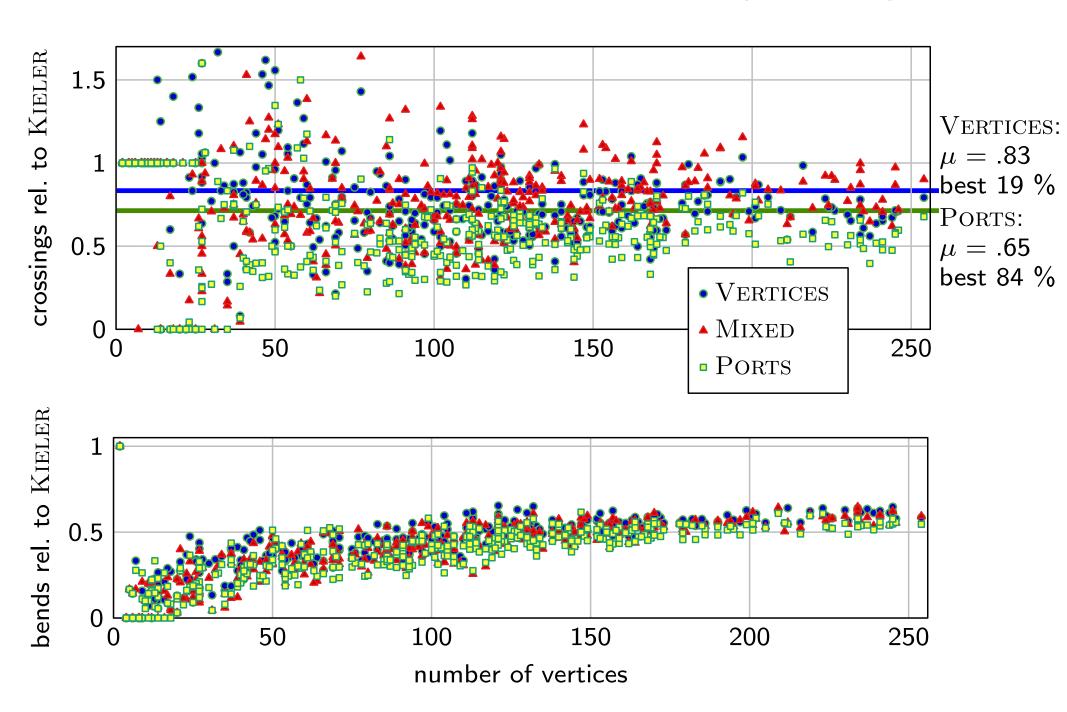


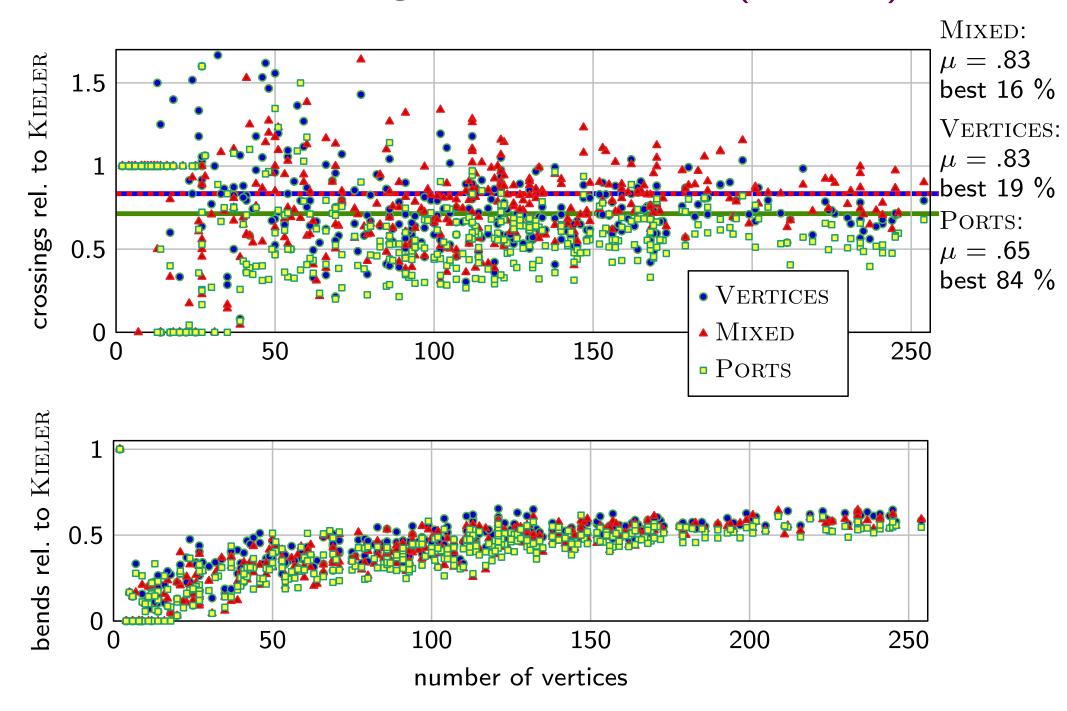
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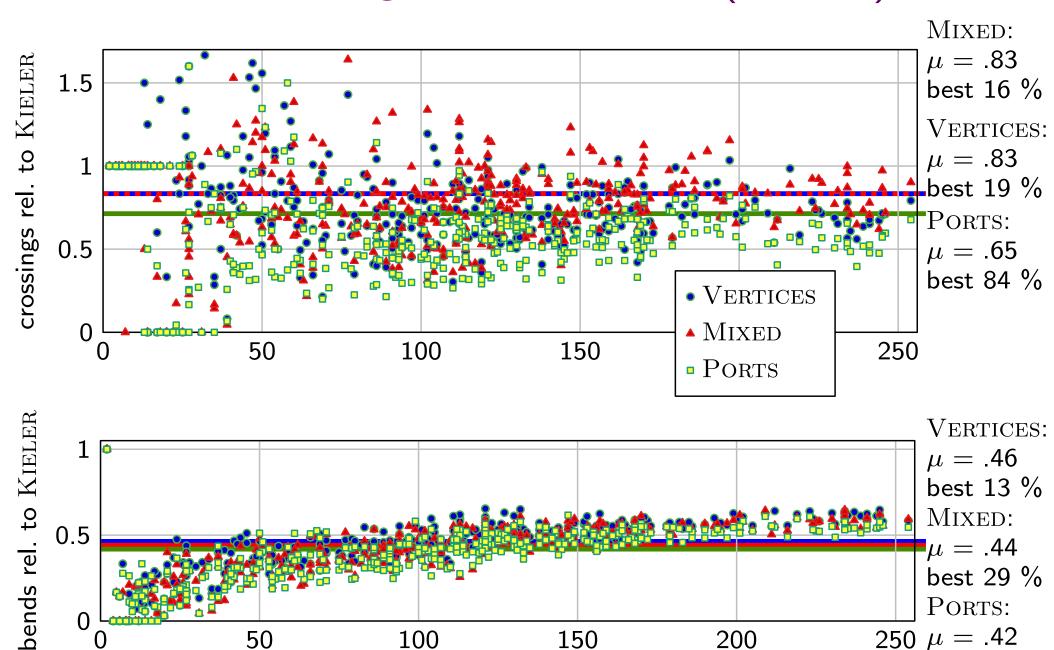






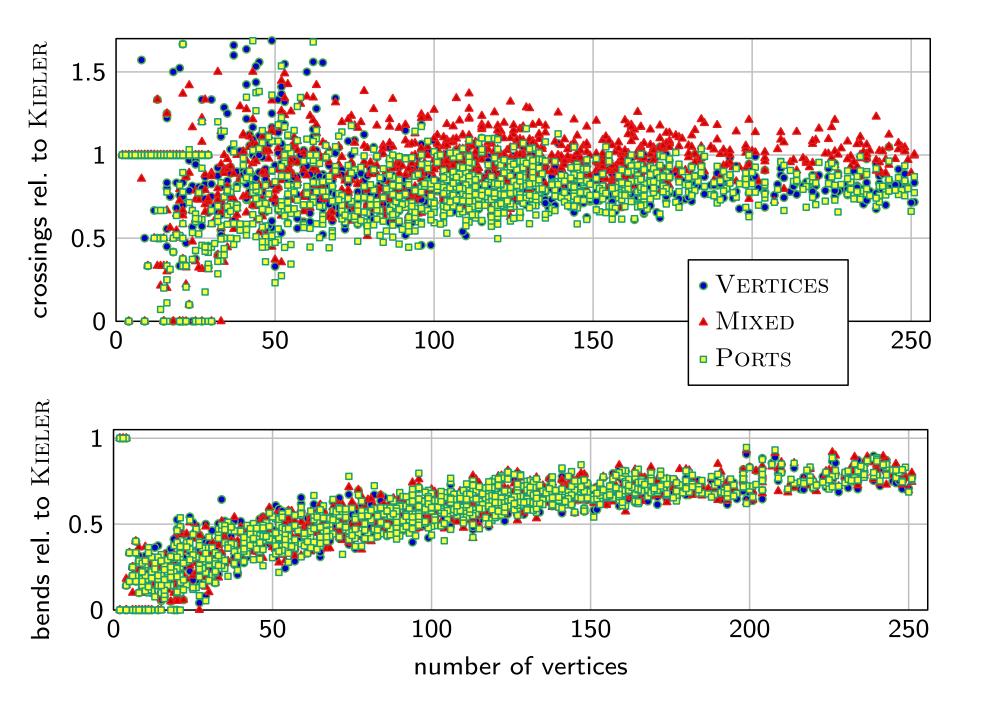
best 72 %

Results: Crossing Minimization (REAL)

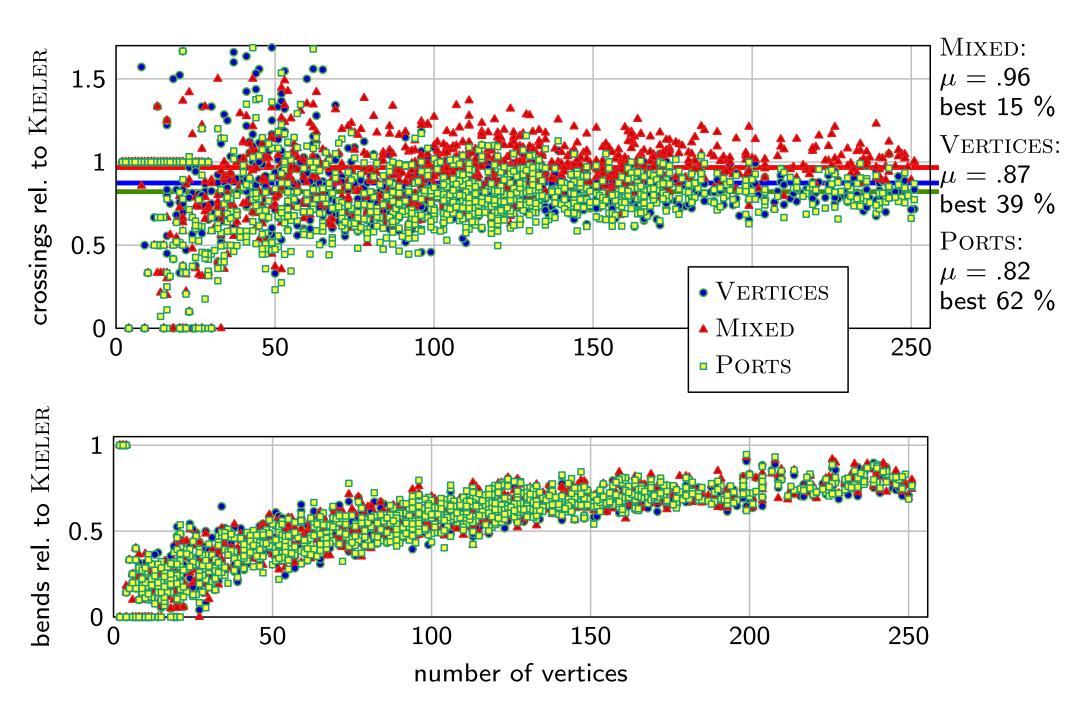


number of vertices

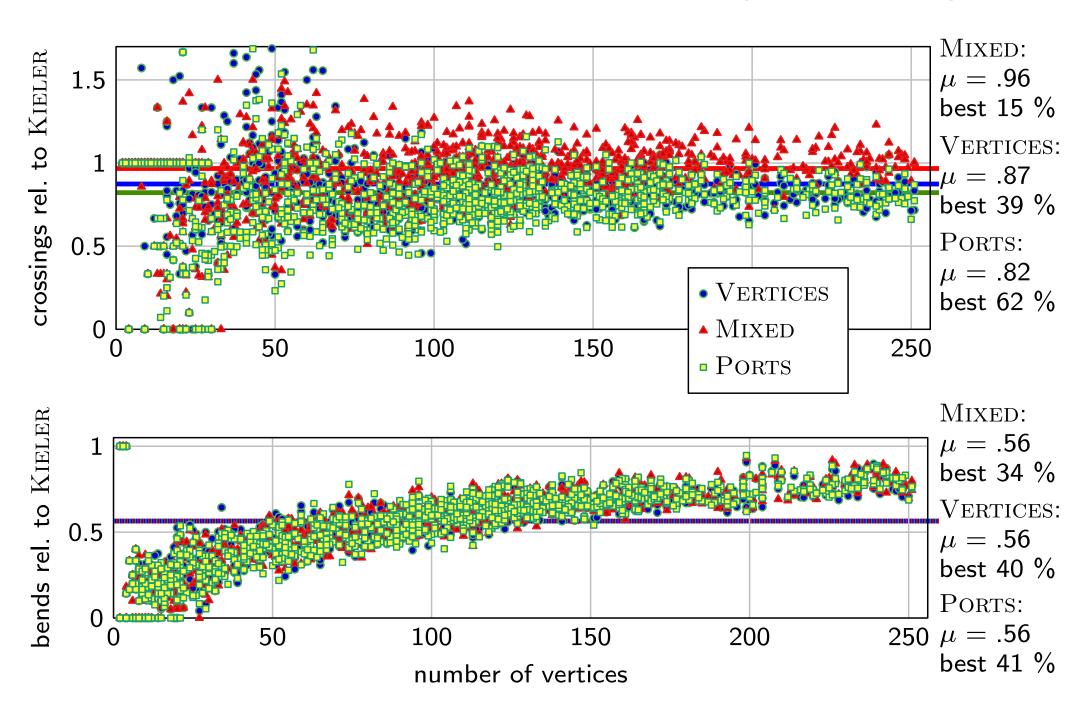
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- Our variants compare well with existing implementation (KIELER) in terms of #crossings and #bends (but slower).
- We intend to integrate our algorithm into the software of our industrial partner to see whether this statistical improvement yields advantages in practice.