



An Optimization-Based Approach for Continuous Map Generalization

Dongliang Peng

Chair of Computer Science I, University of Würzburg, Germany



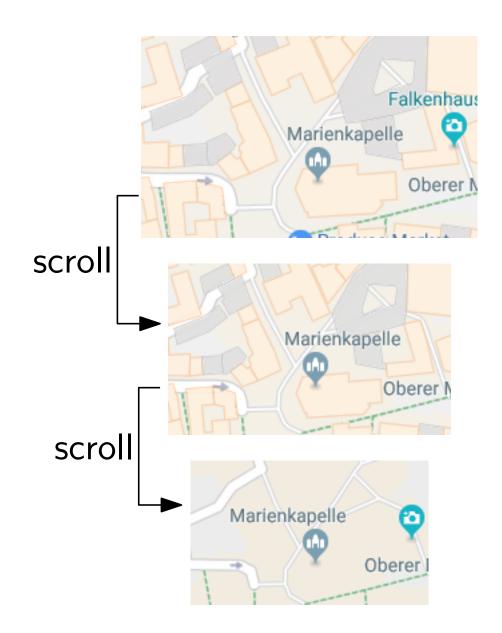


Marienkapelle



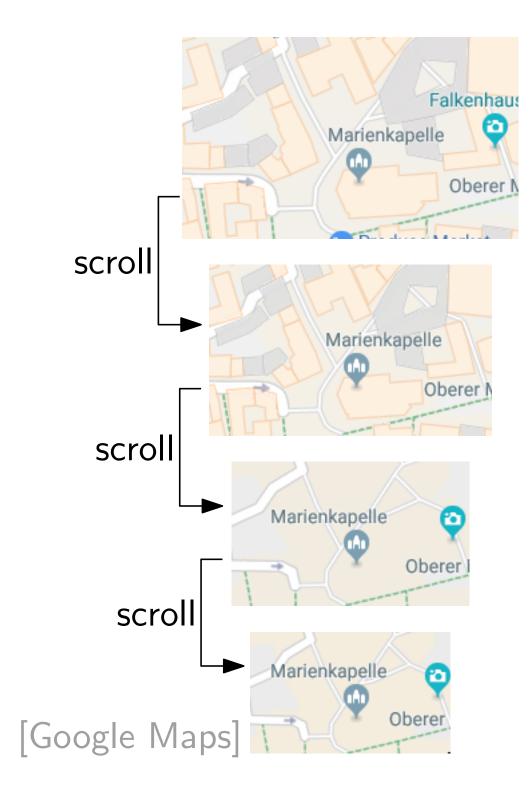


Marienkapelle



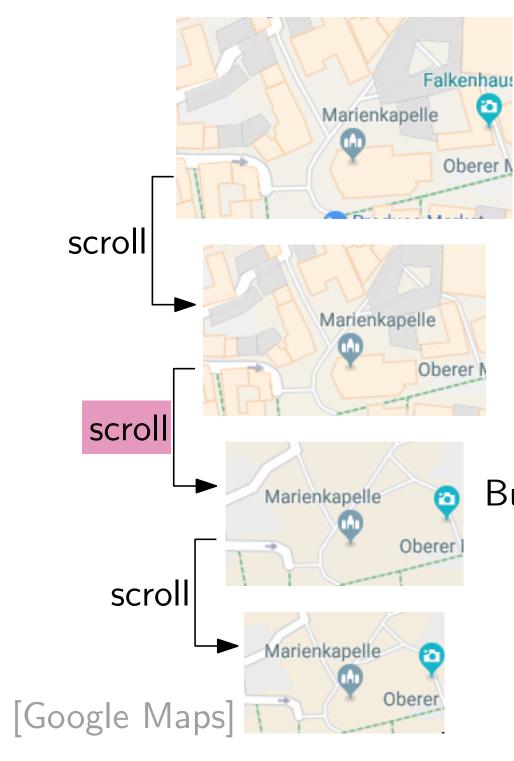


Marienkapelle [source: Wikipedia]





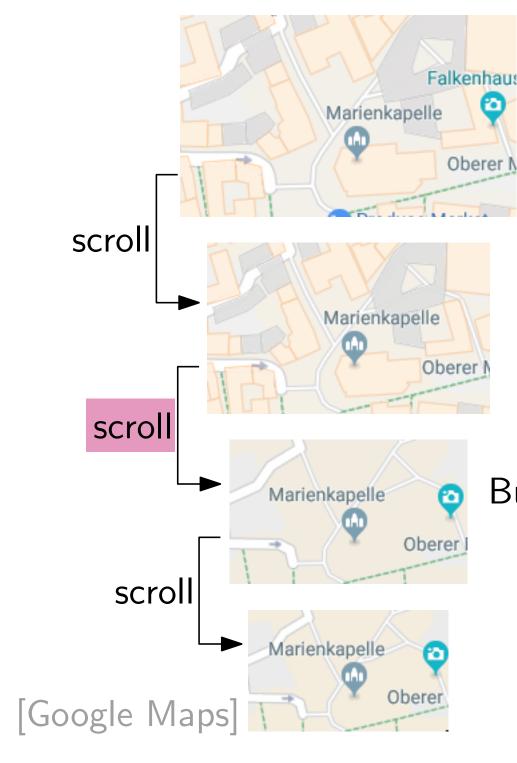
Marienkapelle [source: Wikipedia]





Marienkapelle

Buildings disappear suddenly!





Marienkapelle

Buildings disappear suddenly!

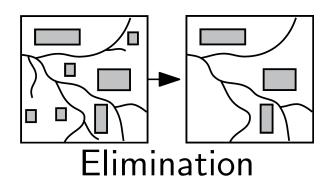
Smooth changes

provide better experience!

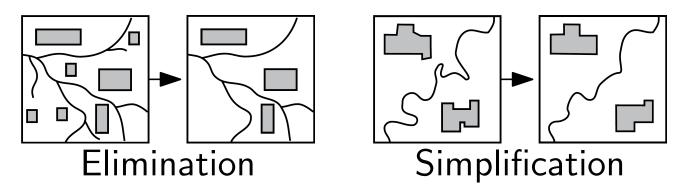
... is about deriving a smaller-scale map from an existing map.

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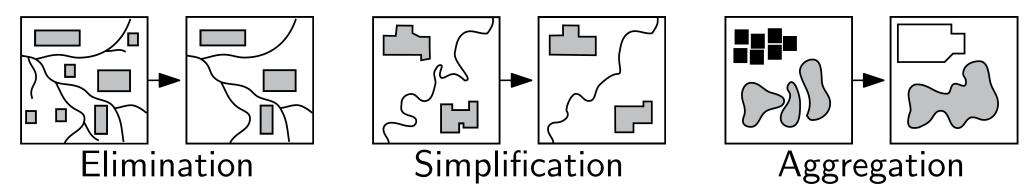
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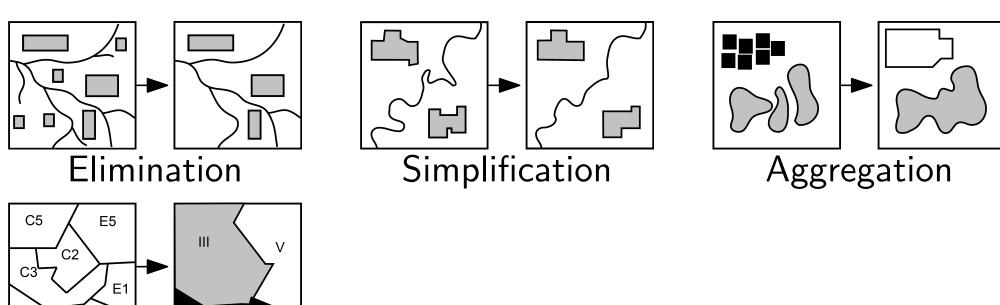


... is about deriving a smaller-scale map from an existing map.



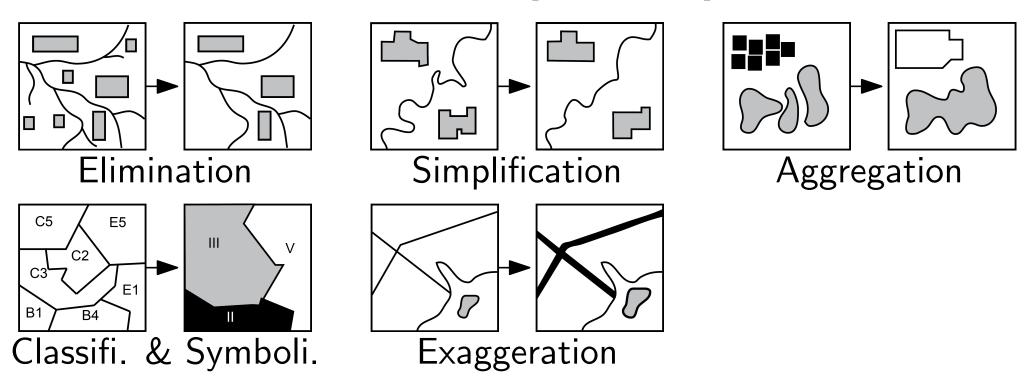
... is about deriving a smaller-scale map from an existing map.

Typical generalization operators [ESRI 1996]:

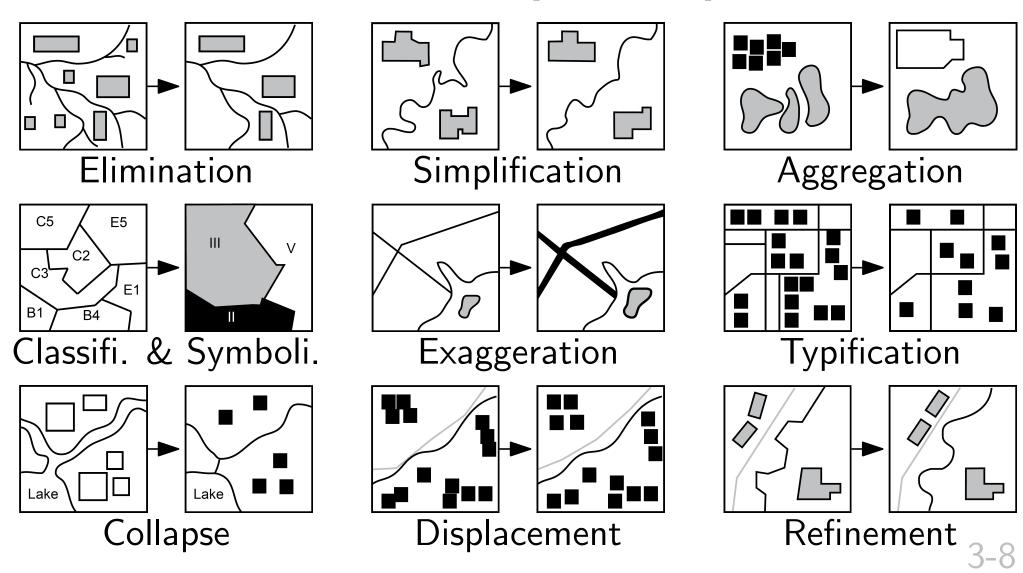


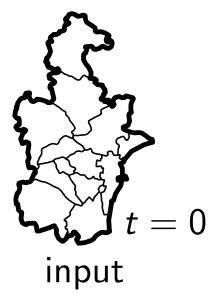
B4

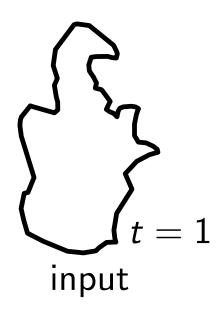
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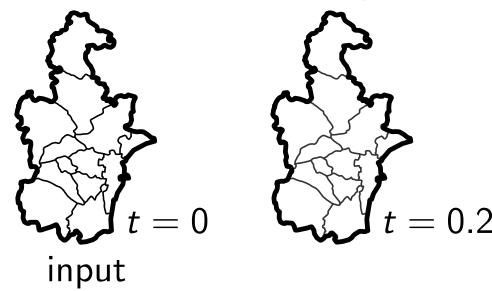


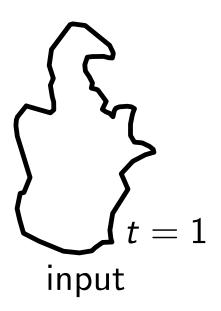
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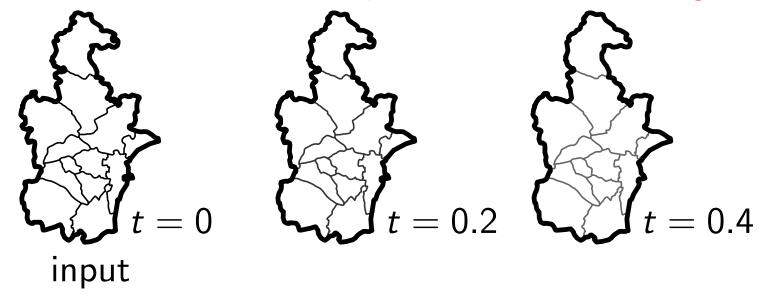


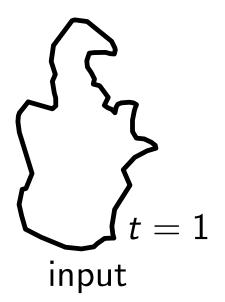


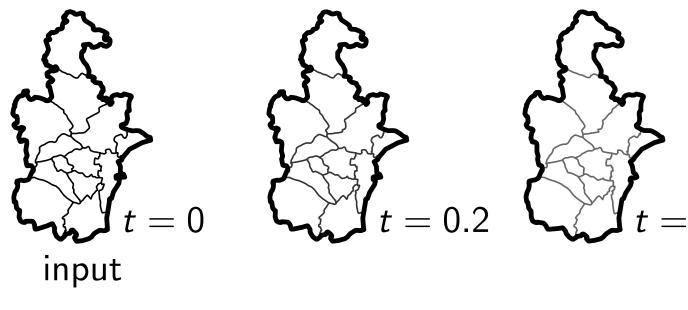


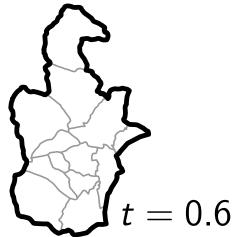


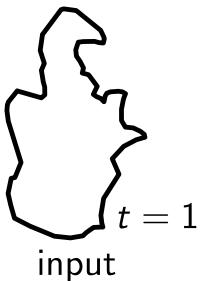


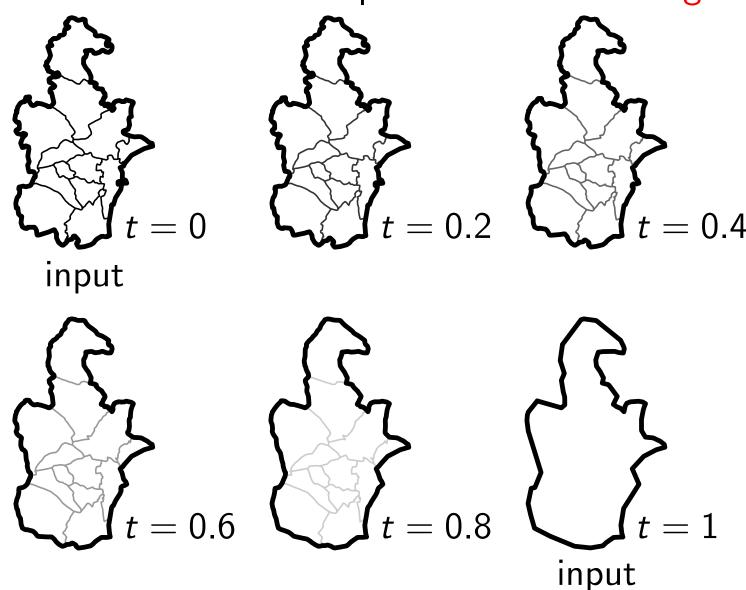






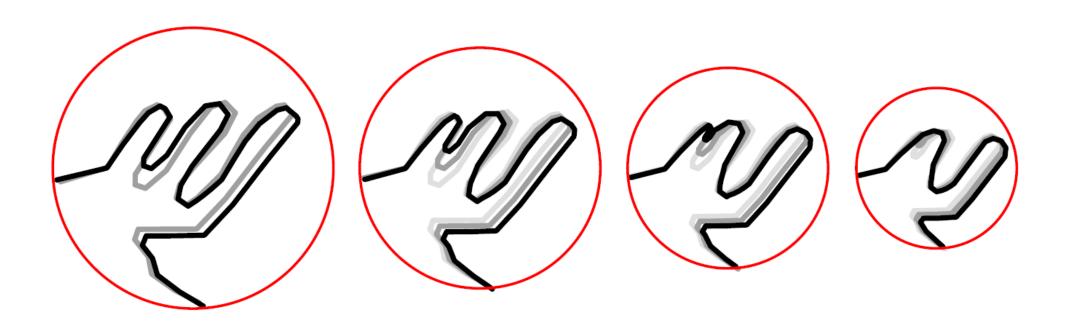






Morph between polylines

[Nöllenburg et al. 2008]



- Morph between polylines
- Generate a good sequence of maps [Chimani et al. 2014]

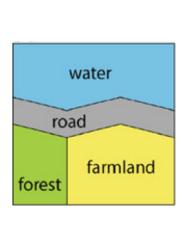
[Nöllenburg et al. 2008]

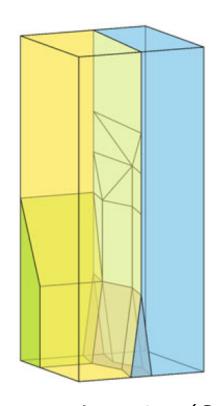


Morph between polylines

- [Nöllenburg et al. 2008]
- Generate a good sequence of maps [Chimani et al. 2014]
- Data structure for continuous generalization

[van Oosterom et al. 2014]



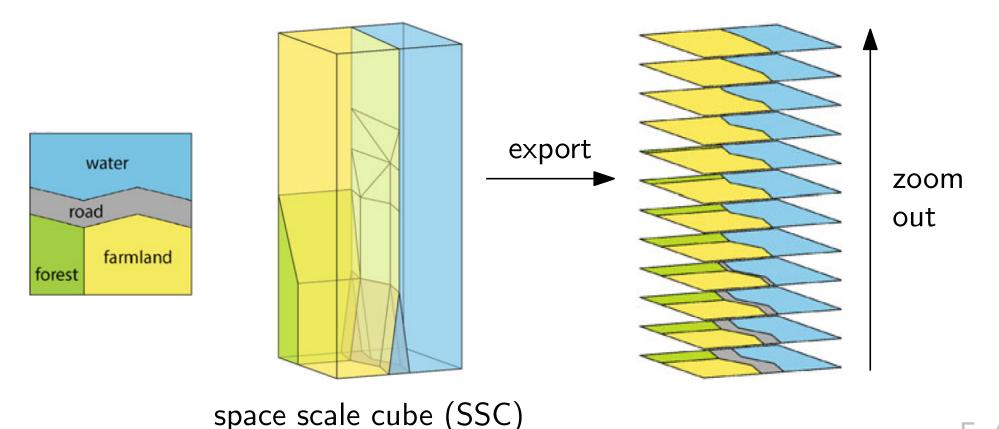


space scale cube (SSC)

Morph between polylines

- [Nöllenburg et al. 2008]
- Generate a good sequence of maps [Chimani et al. 2014]
- Data structure for continuous generalization

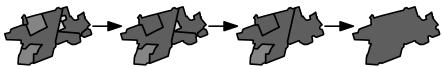
[van Oosterom et al. 2014]



Optim.

Related Generalization

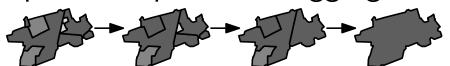
Optimal sequence for aggregation



Optim.

Related Generalization

Optimal sequence for aggregation

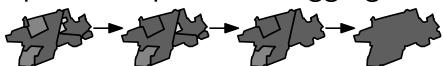


Д* П г

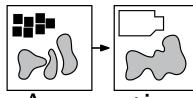
Optim.

Related Generalization

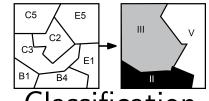
Optimal sequence for aggregation



A* ILP



Aggregation

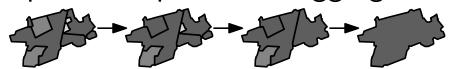


Classification

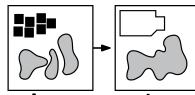
Optim.

Related Generalization

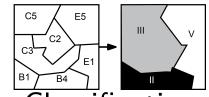
Optimal sequence for aggregation



A* ILP



Aggregation



Classification

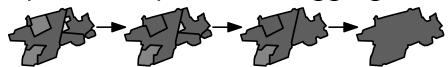
Administrative boundaires



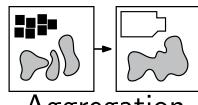
Optim.

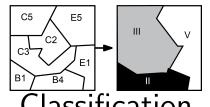
Related Generalization

Optimal sequence for aggregation



 A^{\star} **ILP**





Aggregation

Classification

Administrative boundaires

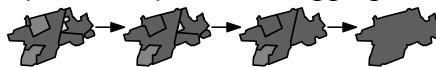


DP

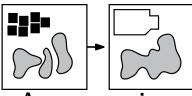
Optim.

Related Generalization

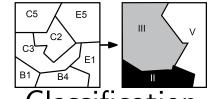
Optimal sequence for aggregation



A* ILP

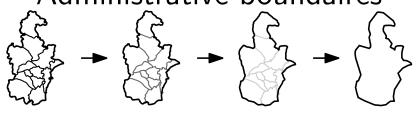


Aggregation

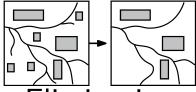


Classification

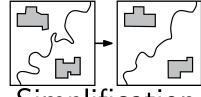
Administrative boundaires



DP



Élimination

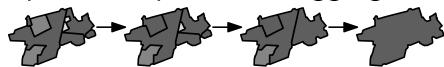


Simplification

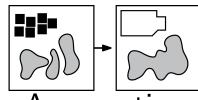
Optim.

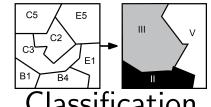
Related Generalization

Optimal sequence for aggregation



 A^{\star} **ILP**





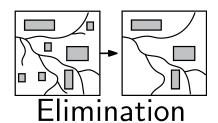
Aggregation

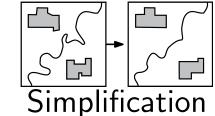
Classification

Administrative boundaires



DP



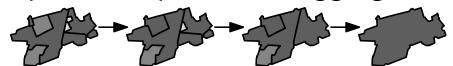


Buildings to built-up areas

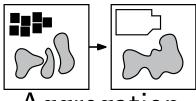
Optim.

Related Generalization

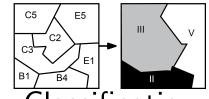
Optimal sequence for aggregation



A* ILP



Aggregation

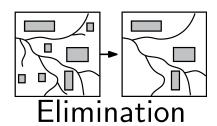


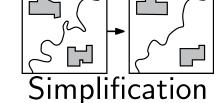
Classification

Administrative boundaires

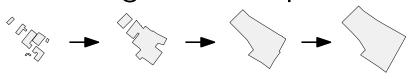


DP





Buildings to built-up areas

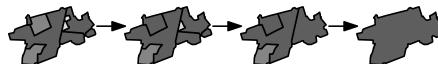


MST

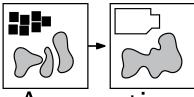
Optim.

Related Generalization

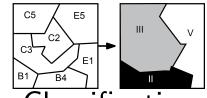
Optimal sequence for aggregation



 A^{\star} **ILP**



Aggregation

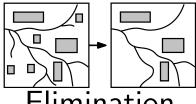


Classification

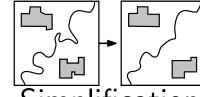
Administrative boundaires



DP

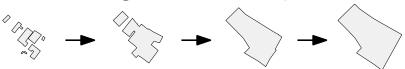


Elimination

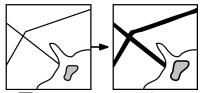


Simplification

Buildings to built-up areas



MST



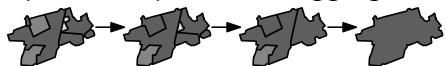
Exaggeration

Aggregation, Simplification, Elimination

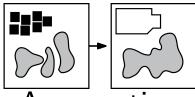
Optim.

Related Generalization

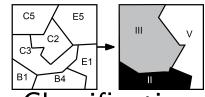
Optimal sequence for aggregation



 A^{\star} **ILP**



Aggregation

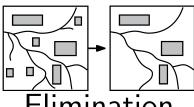


Classification

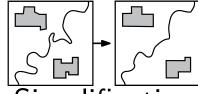
Administrative boundaires



DP



Elimination

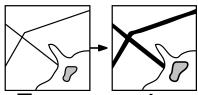


Simplification

Buildings to built-up areas



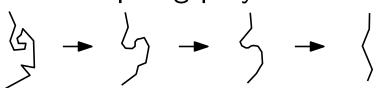
MST



Exaggeration

Aggregation, Simplification, Elimination

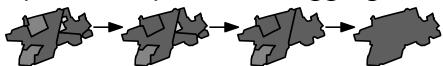
Morphing polylines



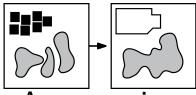
Optim.

Related Generalization

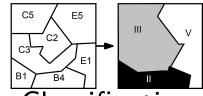
Optimal sequence for aggregation



A* ILP



Aggregation

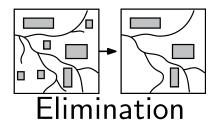


Classification

Administrative boundaires

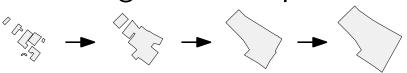


DP

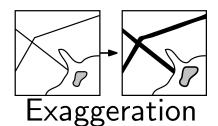


Simplification

Buildings to built-up areas

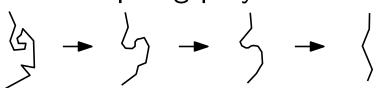


MST



Aggregation, Simplification, Elimination

Morphing polylines

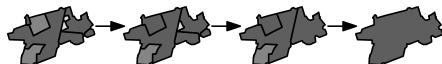


LSA DP

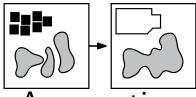
Optim.

Related Generalization

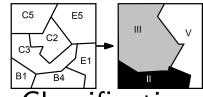
Optimal sequence for aggregation



 A^{\star} **ILP**



Aggregation

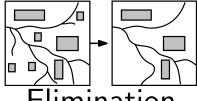


Classification

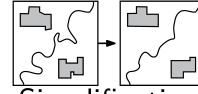
Administrative boundaires



DP

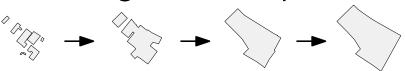


Elimination

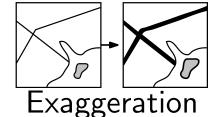


Simplification

Buildings to built-up areas

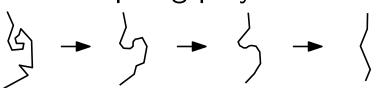


MST

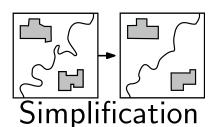


Aggregation, Simplification, Elimination

Morphing polylines



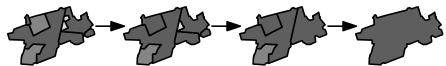
LSA DP



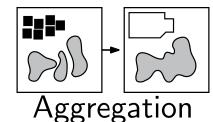
Optim.

Related Generalization

Optimal sequence for aggregation



A* ILP



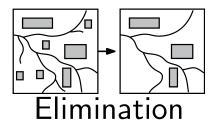
C5 C2 E5 III

Classification

Administrative boundaires



DP

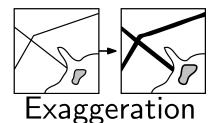


Simplification

Buildings to built-up areas

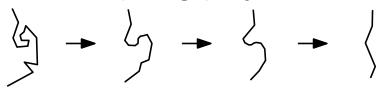


MST

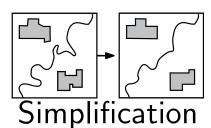


Aggregation, Simplification, Elimination

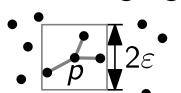
Morphing polylines



LSA DP



Choosing right data structures

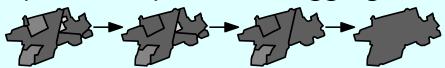


SortedDictionary, SortedSet, . . .

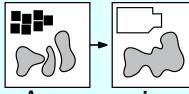
Optim.

Related Generalization

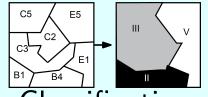
Optimal sequence for aggregation



A* ILP



Aggregation

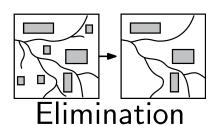


Classification

Administrative boundaires

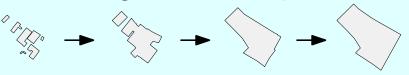


DP

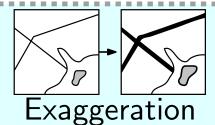


Simplification

Buildings to built-up areas



MST

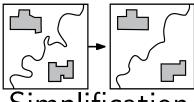


Aggregation, Simplification, Elimination

Morphing polylines

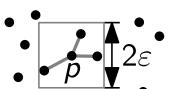


LSA DP



Simplification |

Choosing right data structures

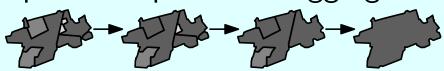


SortedDictionary, SortedSet, . . .

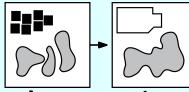
Optim.

Related Generalization

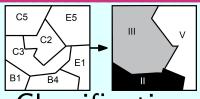
Optimal sequence for aggregation



A* ILP



Aggregation

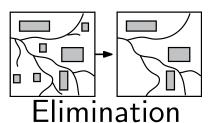


Classification

Administrative boundaires

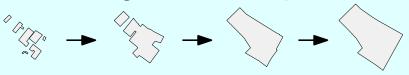


DP

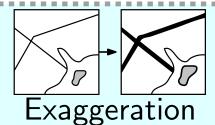


Simplification

Buildings to built-up areas

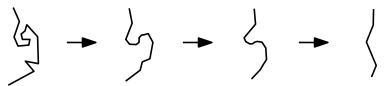


MST

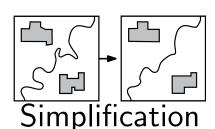


Aggregation, Simplification, Elimination

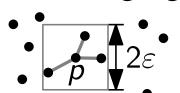
Morphing polylines



LSA DP

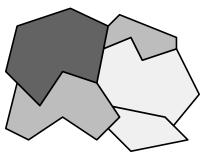


Choosing right data structures

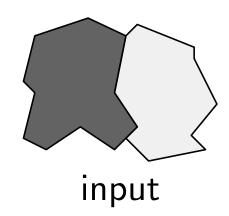


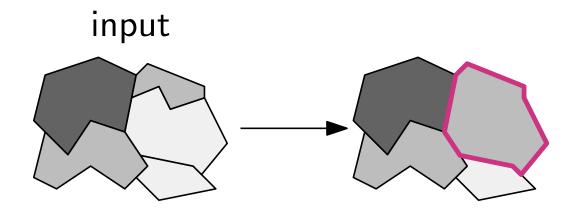
SortedDictionary, SortedSet, . . .

input

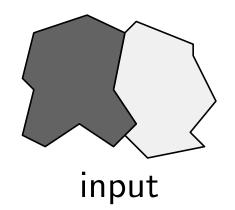


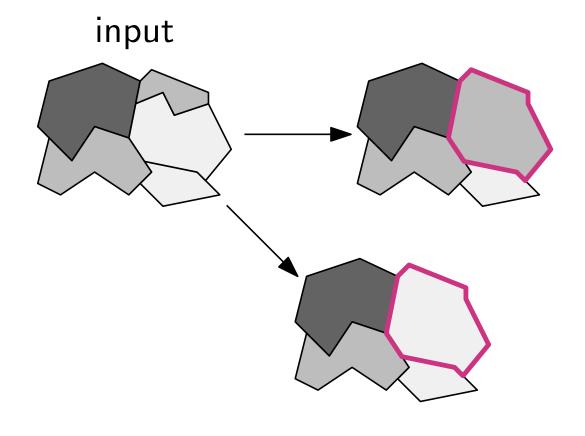




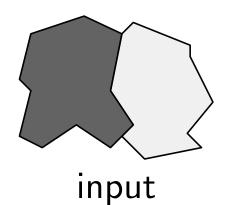


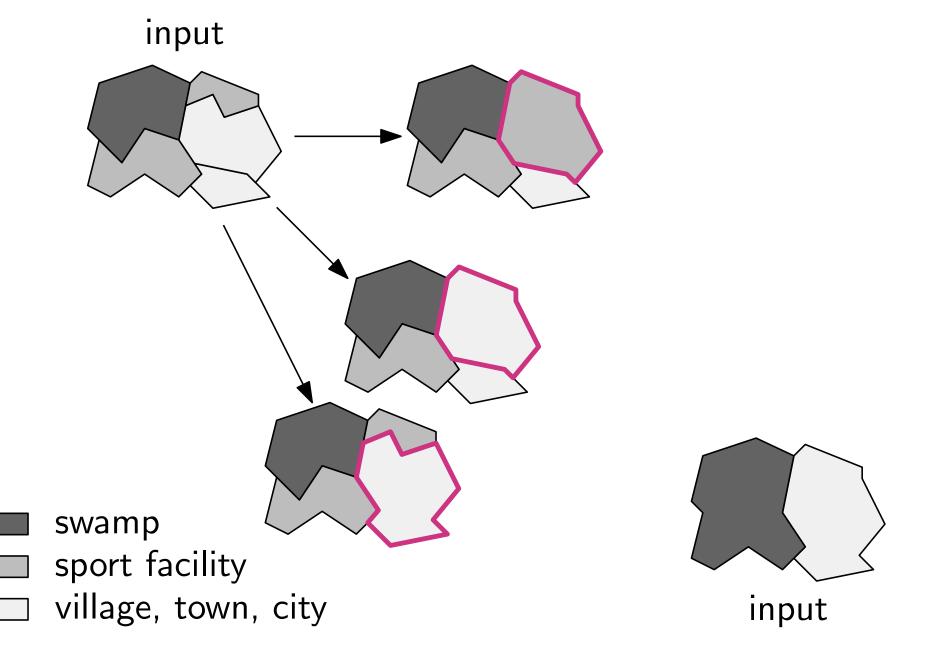
swampsport facilityvillage, town, city

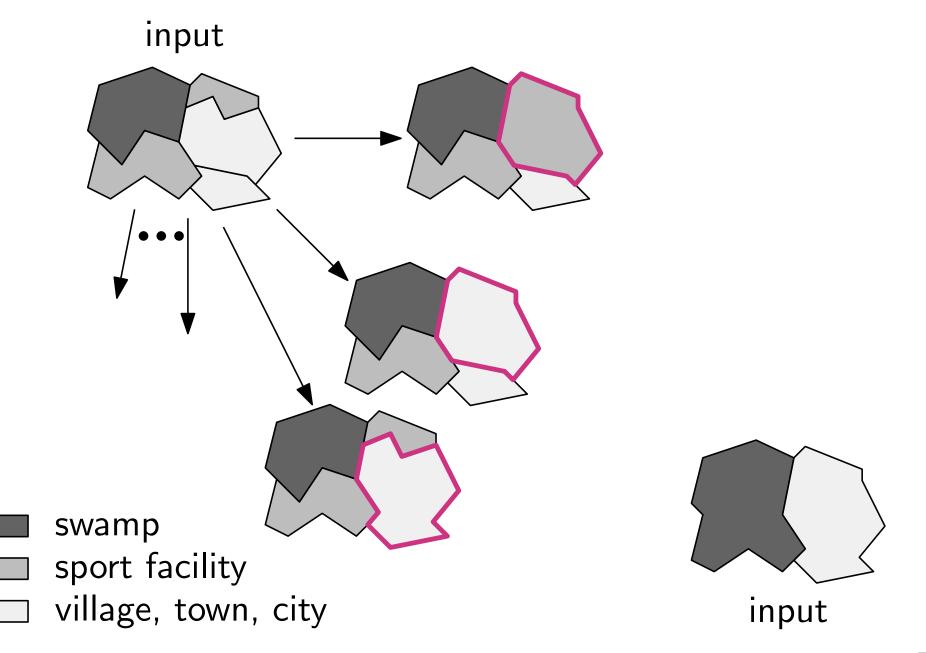


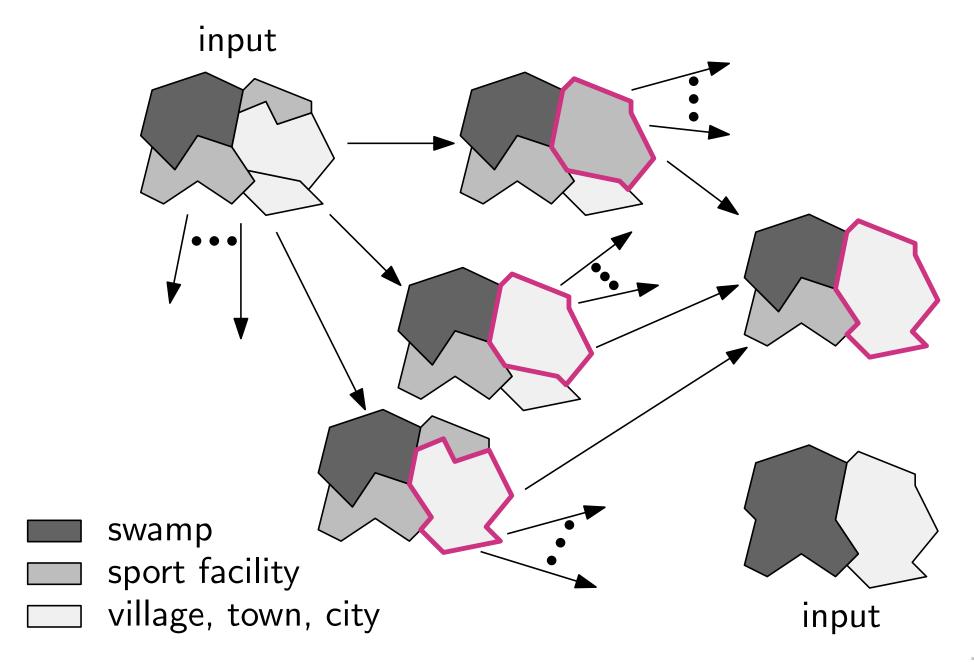


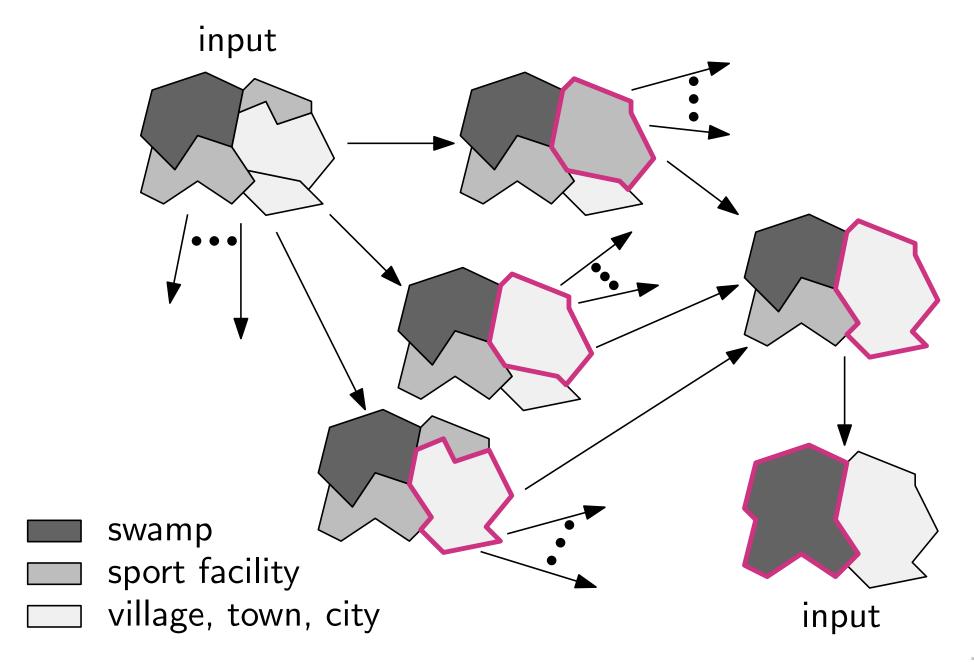
- **swamp**
- sport facility
- ____ village, town, city

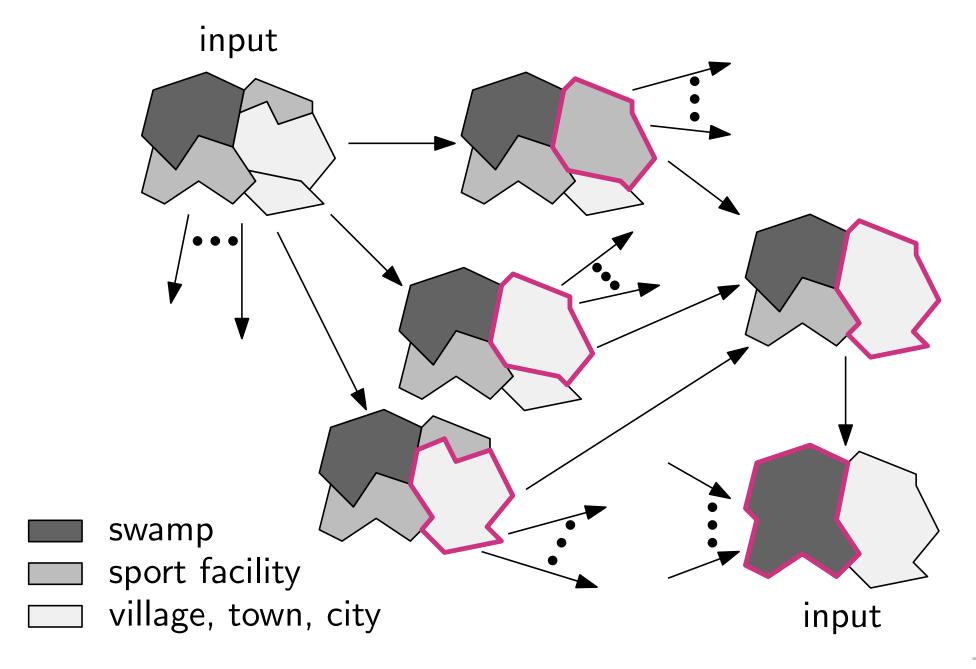




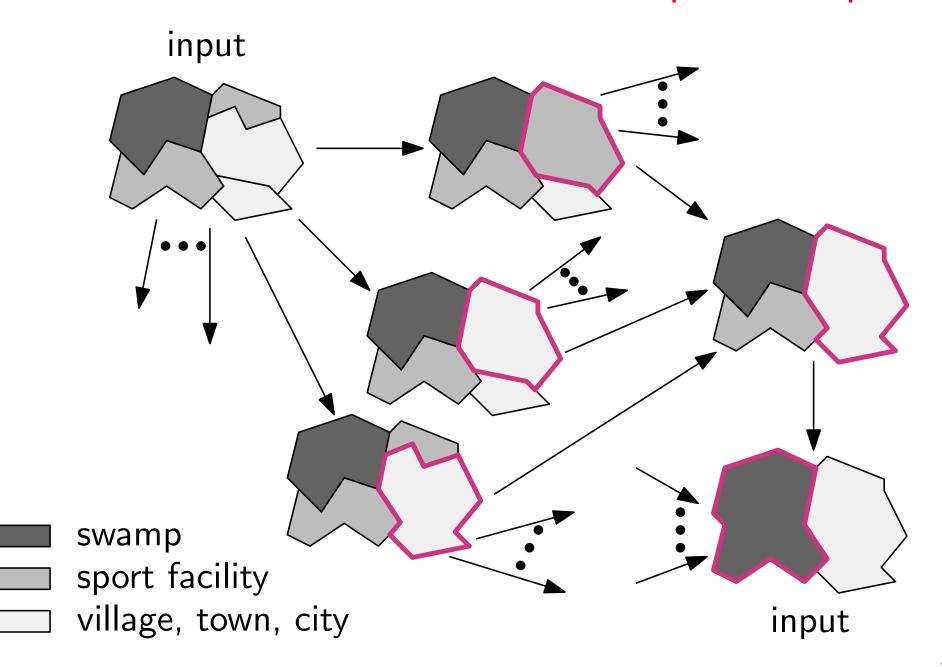


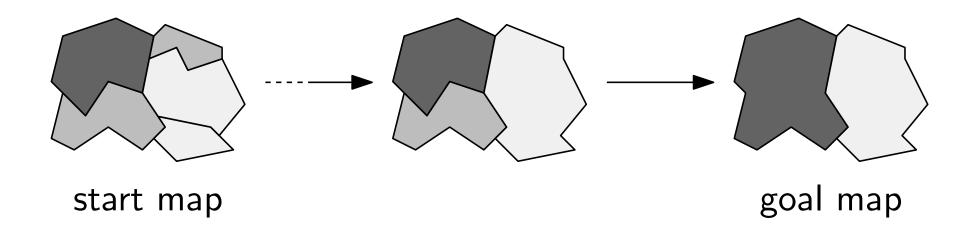




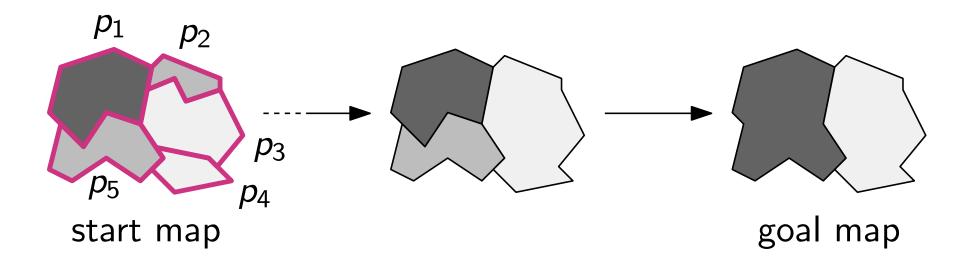


Given aggregation costs: What is an optimal sequence?



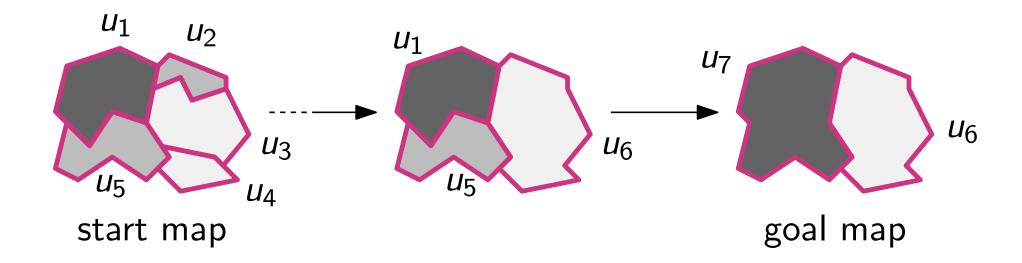


Polygon p_i : area on start map



Polygon p_i : area on start map

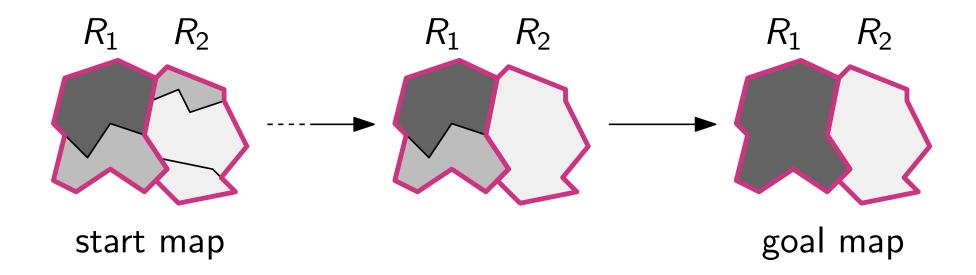
Patch u_i : connected set of areas



Polygon p_i : area on start map

Patch u_i : connected set of areas

Region R_i : area on the goal map

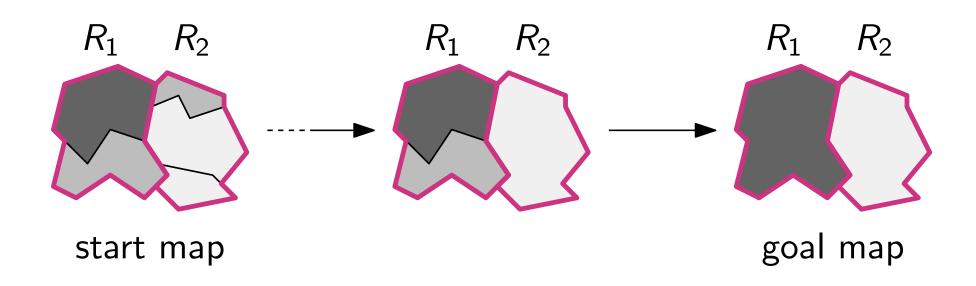


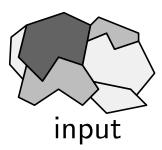
Polygon p_i : area on start map

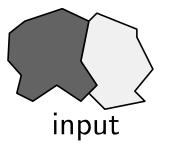
Patch u_i : connected set of areas

Region R_i : area on the goal map

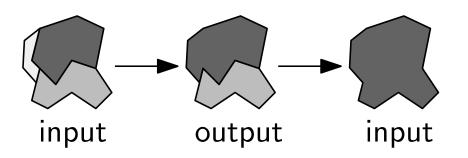
Aggregate the smallest patch with its neighbour

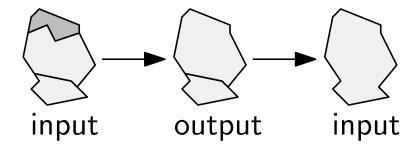


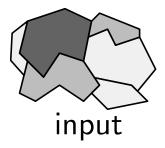


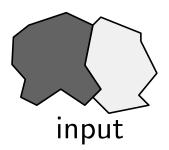


Compute a sequence for each region

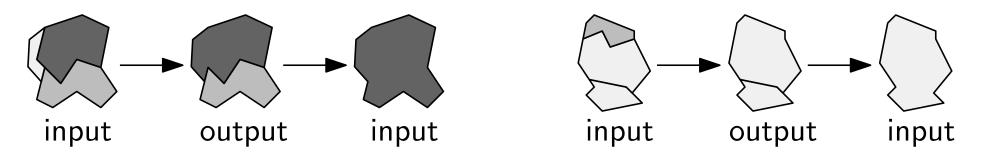






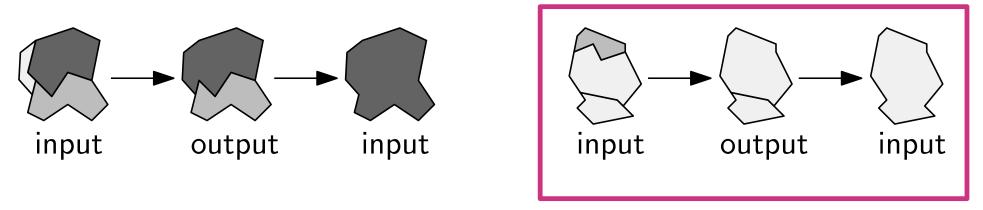


Compute a sequence for each region



Interleave according to order of smallest areas (as merge sort)

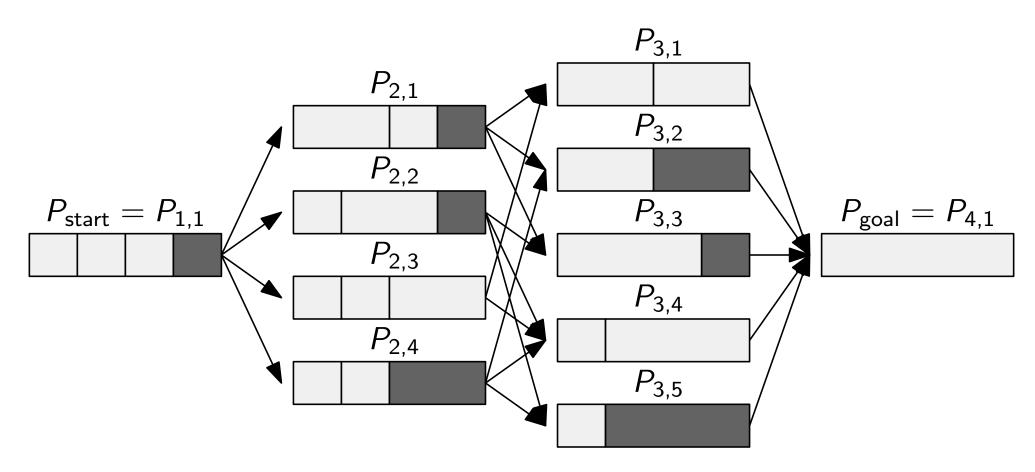
Compute a sequence for each region



Interleave according to order of smallest areas (as merge sort)

Subdivision

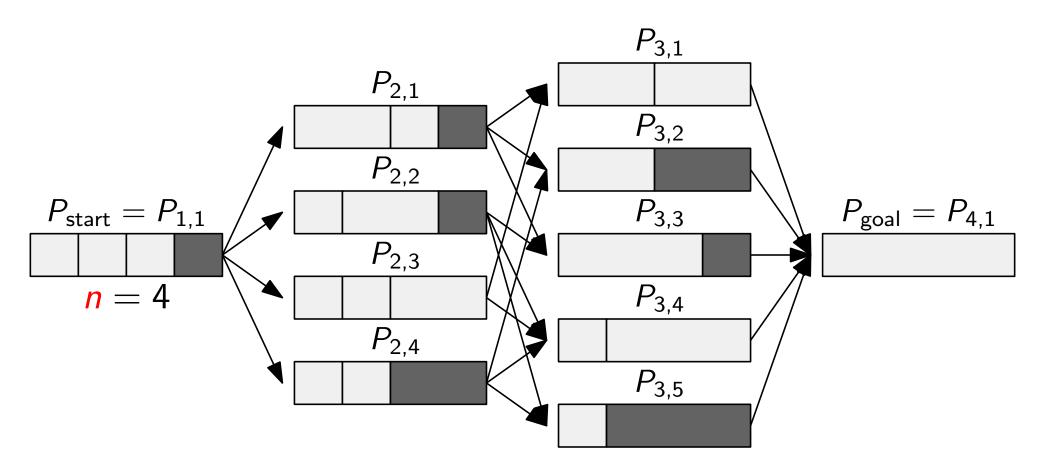
Subdivision $P_{t,i}$: patches subdividing a region



Subdivision

Subdivision $P_{t,i}$: patches subdividing a region

Size *n* : #polygons on start map

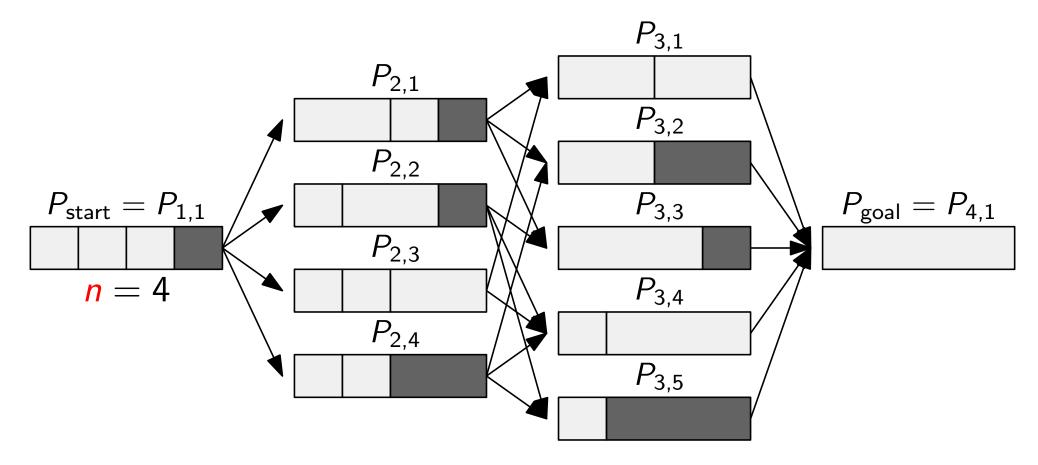


Subdivision

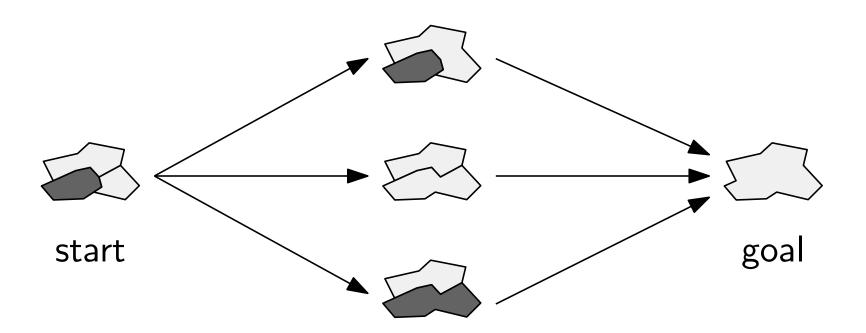
Subdivision $P_{t,i}$: patches subdividing a region

Size *n* : #polygons on start map

#subdivions is exponential in n.

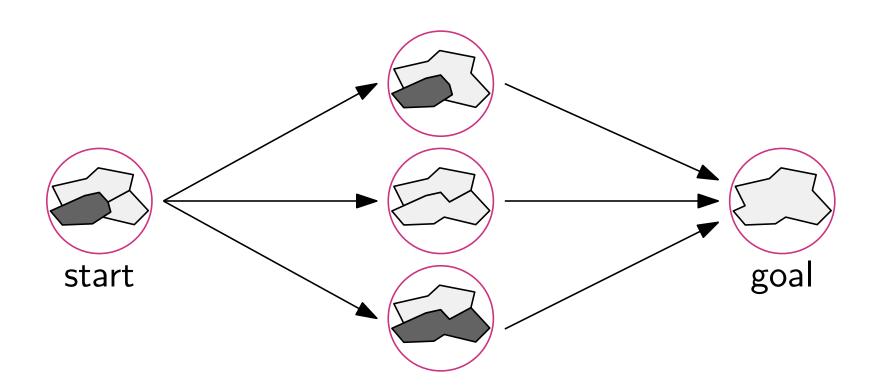


Formalizing a Pathfinding Problem



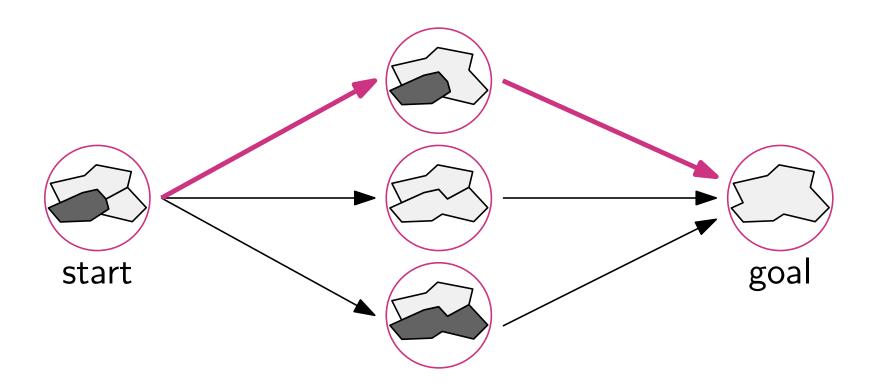
Formalizing a Pathfinding Problem

• Each subdivision is represented as a node

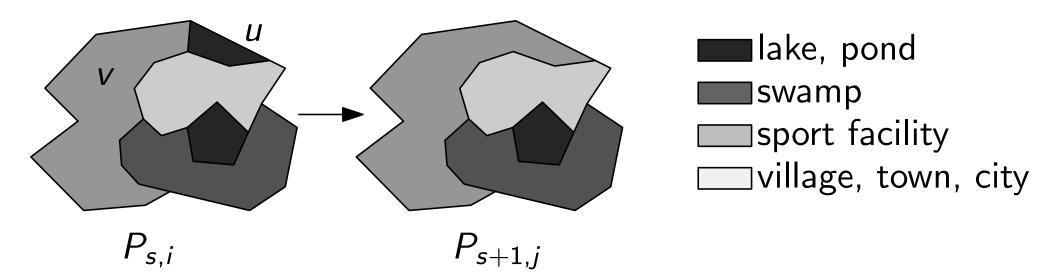


Formalizing a Pathfinding Problem

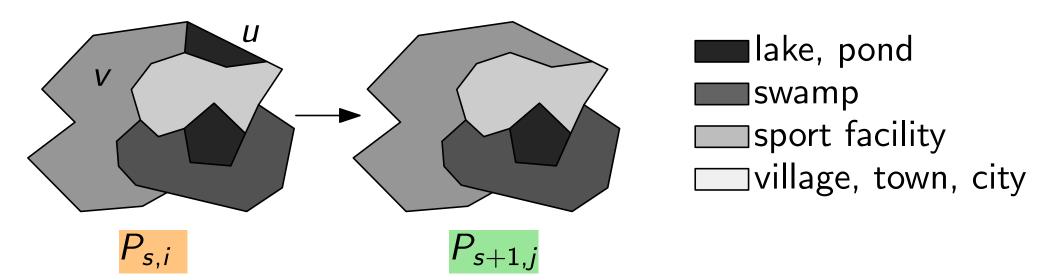
- Each subdivision is represented as a node
- Find a shortest path w.r.t. cost functions



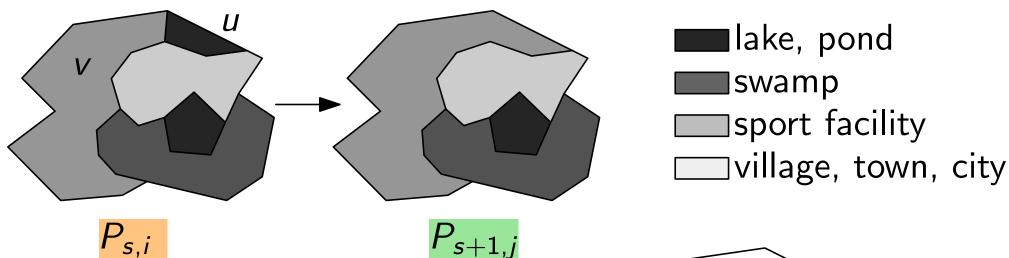
• Type change: $f_{\text{type}}(P_{s,i}, P_{s+1,j})$ We wish to aggregate patches with similar types



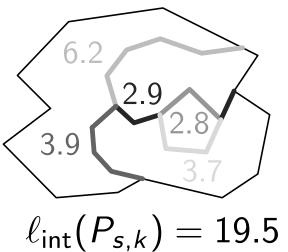
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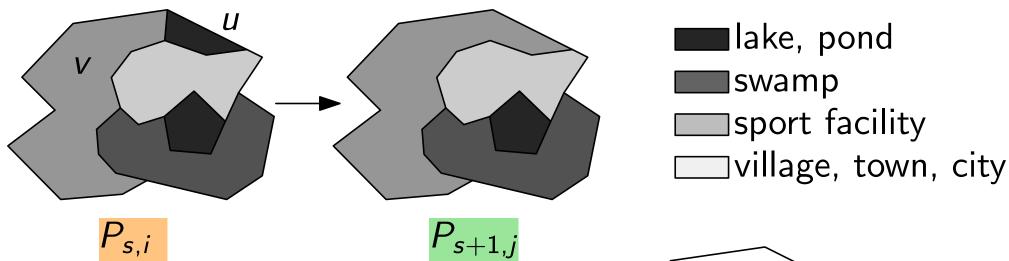
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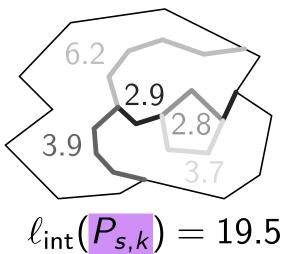
• Interior length: $f_{length}(P_{s,k})$ Less length, easier to perceive



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• Path $\Pi = (P_{1,i_1}, P_{2,i_2}, \dots, P_{t,i_t})$

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$$egin{aligned} egin{aligned} f_{ ext{type}}(P_{s,i_s},P_{s+1,i_{s+1}}) \ egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} egin{aligned} f_{ ext{length}}(P_{s,i_s}) \ \end{pmatrix} \end{aligned}$$

• Path $\Pi = (P_{1,i_1}, P_{2,i_2}, \dots, P_{t,i_t})$

$$egin{aligned} oldsymbol{g}_{ ext{type}}(\Pi) &= \sum_{s=1}^{t-1} f_{ ext{type}}(P_{s,i_s},P_{s+1,i_{s+1}}) \ oldsymbol{g}_{ ext{length}}(\Pi) &= \sum_{s=2}^{t-1} f_{ ext{length}}(P_{s,i_s}) \end{aligned}$$

Combination of the two costs:

$$g(\Pi) = (1 - \lambda)g_{\mathsf{type}}(\Pi) + \lambda g_{\mathsf{length}}(\Pi)$$

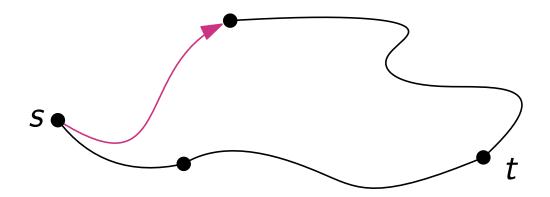
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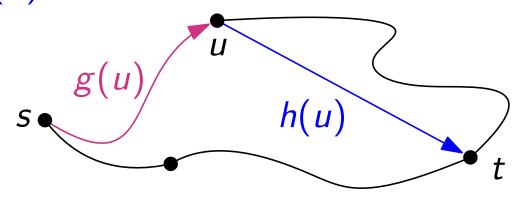
Combination of the two costs:

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 $\lambda = 0.5$

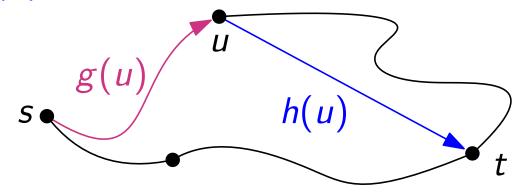
• A best-first search algorithm. Find a path from s to t



- A best-first search algorithm. Find a path from s to t
- Cost function: F(u) = g(u) + h(u)
 - -g(u): exact cost of s-u path
 - -h(u): estimated cost of shortest u-t path

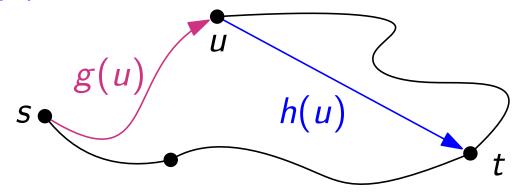


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• Guarantees a shortest path if h(u) is smaller than real cost

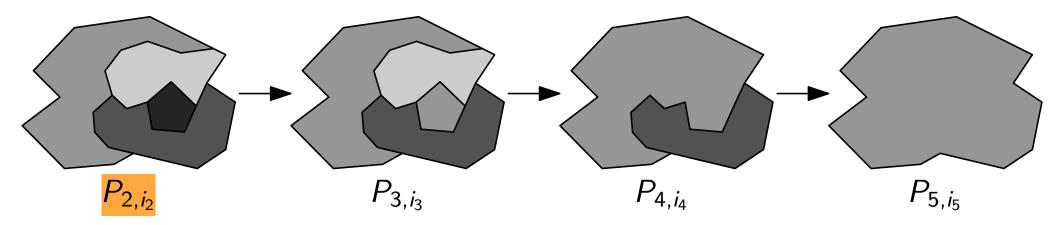
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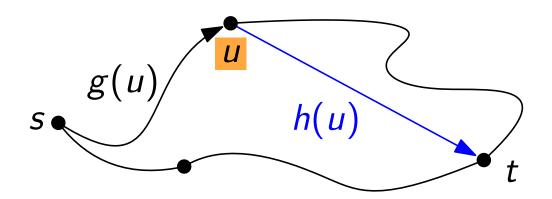


- Guarantees a shortest path if h(u) is smaller than real cost
- Helps ignore some paths

Estimating Cost

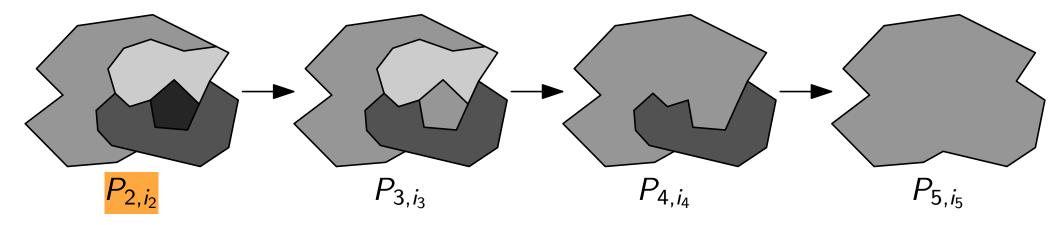
• $h_{\text{type}}(P_{t,i}) = \sum_{s=t}^{n-1} f_{\text{type}}(P_{s,i_s}, P_{s+1,i_{s+1}})$ We assume: Each patch immediately gets the target type.



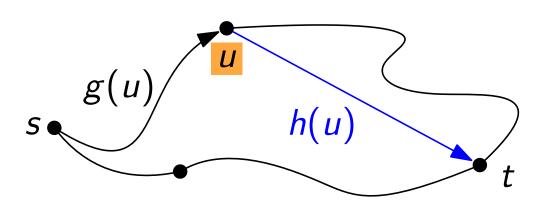


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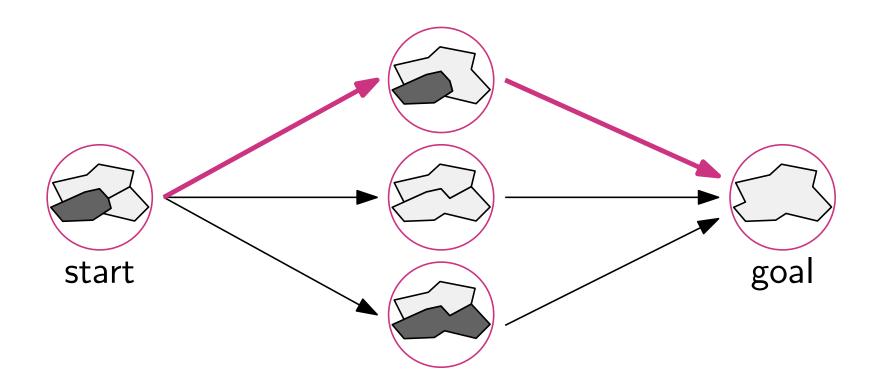


• $h_{\text{length}}(P_{t,i})$



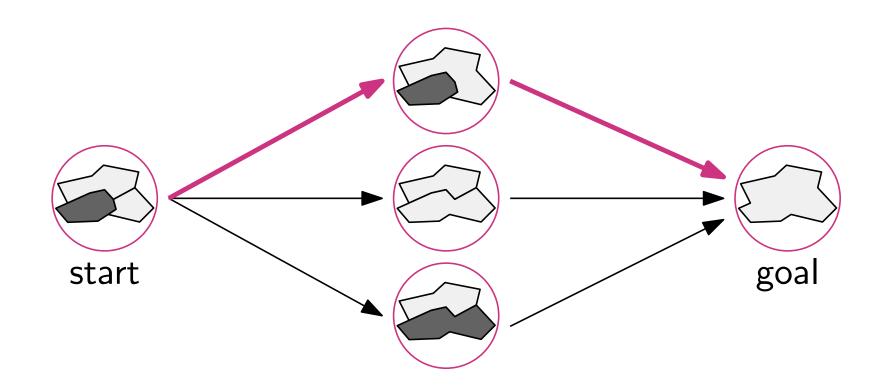
Overestimation

• Try finding a path by exploring at most M = 200,000 nodes. If fail, try again but increasing estimated costs.



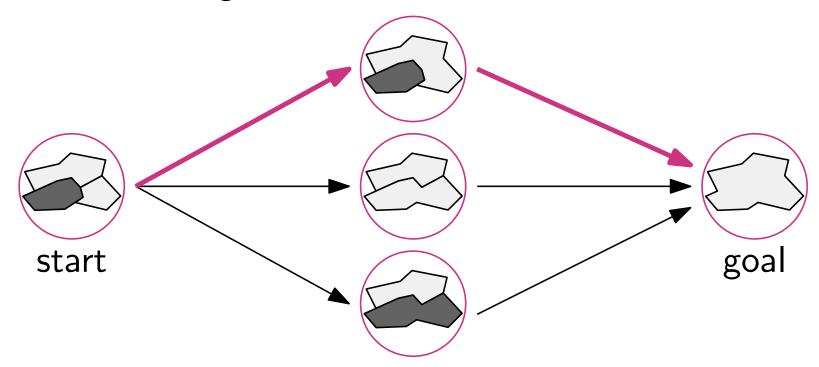
Overestimation

- Try finding a path by exploring at most M=200,000 nodes. If fail, try again but increasing estimated costs.
- A path seems more expensive, thus may be ignored



Overestimation

- Try finding a path by exploring at most M=200,000 nodes. If fail, try again but increasing estimated costs.
- A path seems more expensive, thus may be ignored
- Not optimal anymore once increasing estimated costs



Integer Linear Programming

Form of an integer linear program (ILP)

```
minimize C^{\mathsf{T}}x
subject to Ex \leq H, x \geq \mathbf{0}, and x \in \mathbb{Z}^I,
```

Integer Linear Programming

Form of an integer linear program (ILP)

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Given variables x, minimize a cost subject to some constraints.

Integer Linear Programming

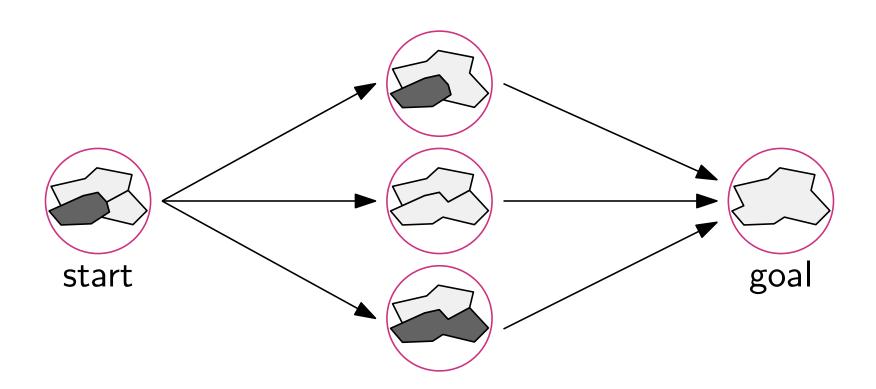
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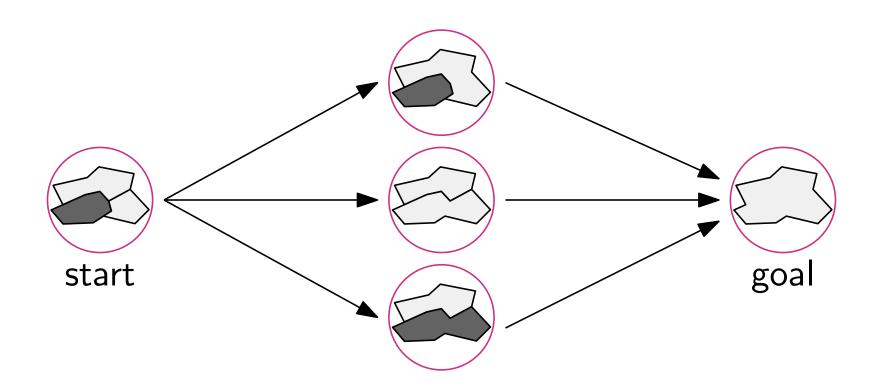
Using Integer Linear Programming

Model complete graph by setting variables and constraints



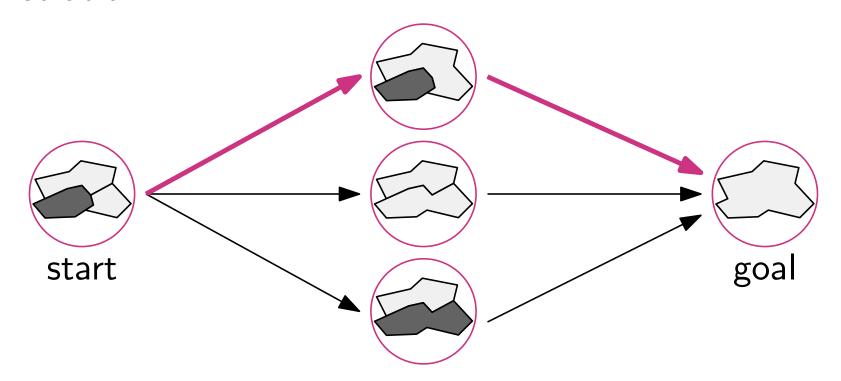
Using Integer Linear Programming

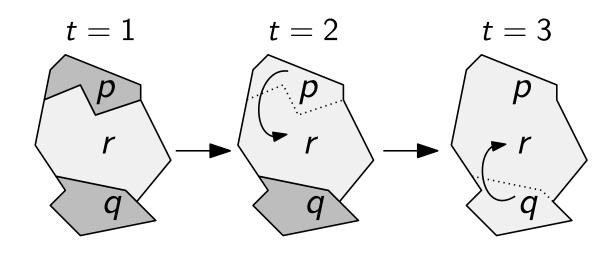
- Model complete graph by setting variables and constraints
- Solve ILP with minimizing total cost

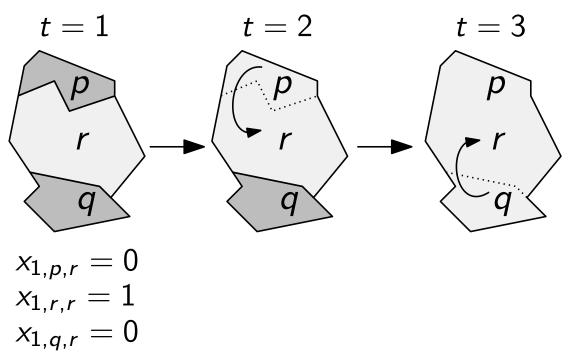


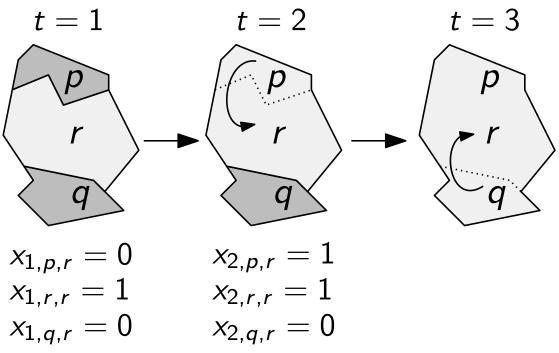
Using Integer Linear Programming

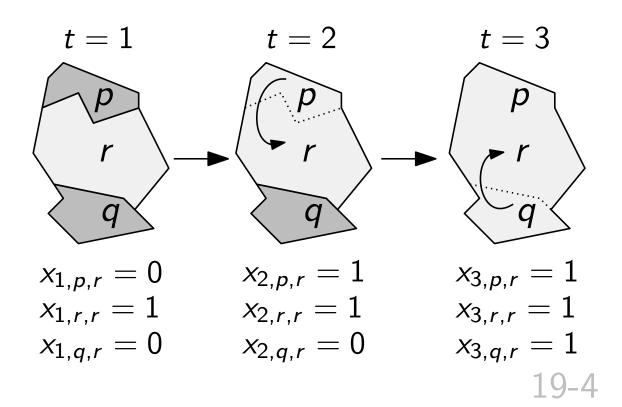
- Model complete graph by setting variables and constraints
- Solve ILP with minimizing total cost
- Define path according to values of variables, known from solution





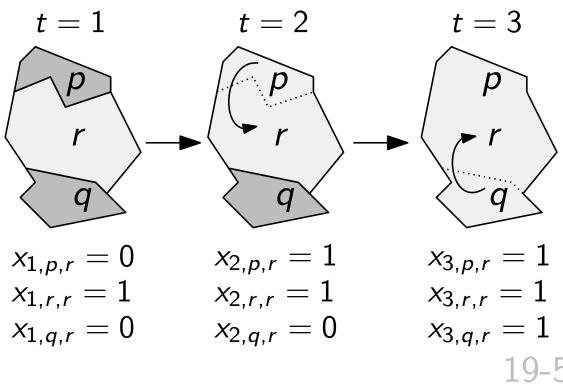






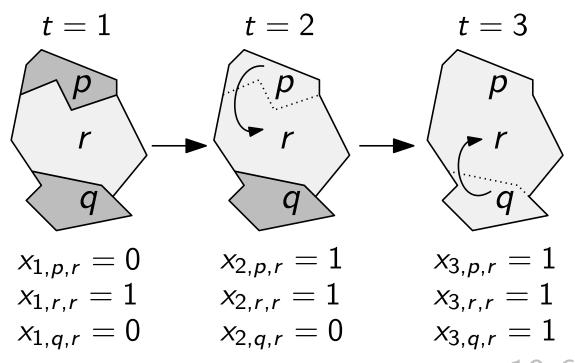
- Variable: $x_{t,p,r} \in \{0,1\}$ $\forall t \in T, \forall p, r \in P$ $x_{t,p,r} = 1 \Leftrightarrow p$ is assigned to r at time t.
- Constraints:

p is assigned to only one polygon: $\sum_{r \in P} x_{t,p,r} = 1$



- Variable: $x_{t,p,r} \in \{0,1\}$ $\forall t \in T, \forall p, r \in P$ $x_{t,p,r} = 1 \Leftrightarrow p$ is assigned to r at time t.
- Constraints:

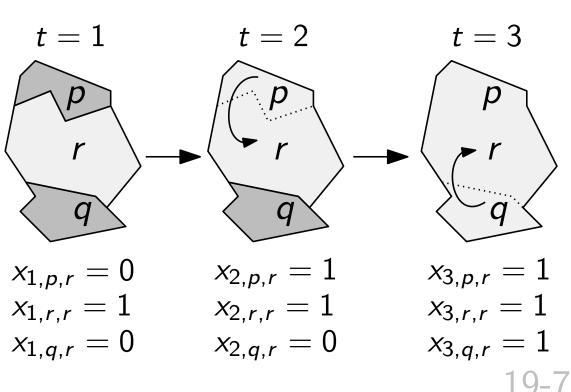
p is assigned to only one polygon: $\sum_{r \in P} x_{t,p,r} = 1$ Enforce aggregation: $\sum_{r \in P} x_{t,r,r} = n - t + 1$



- Variable: $x_{t,p,r} \in \{0,1\}$ $\forall t \in T, \forall p, r \in P$ $x_{t,p,r} = 1 \Leftrightarrow p$ is assigned to r at time t.
- Constraints:

p is assigned to only one polygon: $\sum_{r \in P} x_{t,p,r} = 1$ Fnforce aggregation: $\sum_{r \in P} x_{t,r,r} = n - t + 1$

• In total, 5 sets of variables 17 sets of constraints



Case Study

• Environment: C#, CPLEX

Case Study

• Environment: C#, CPLEX

scale 1:50 k

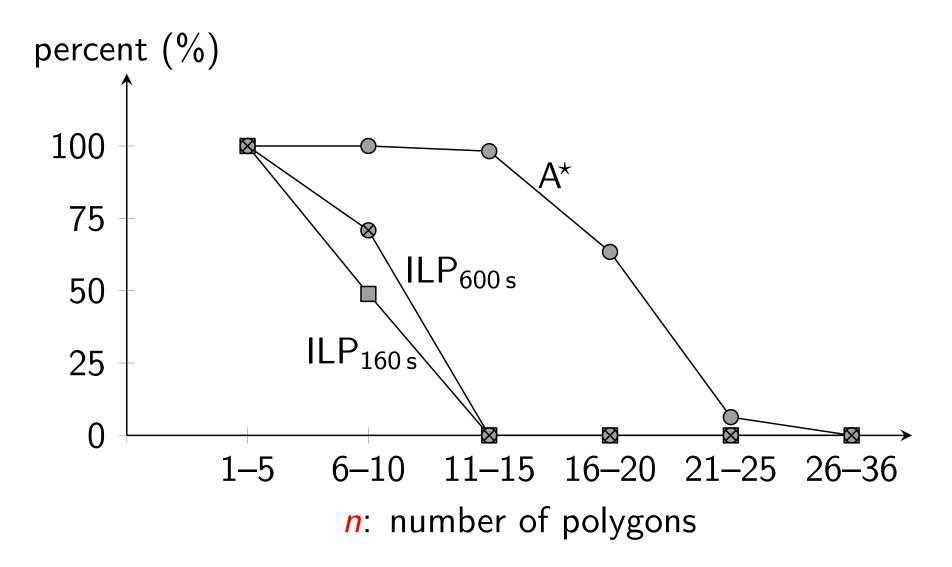
Data 3 km 5,448 patches 734 patches (regions)

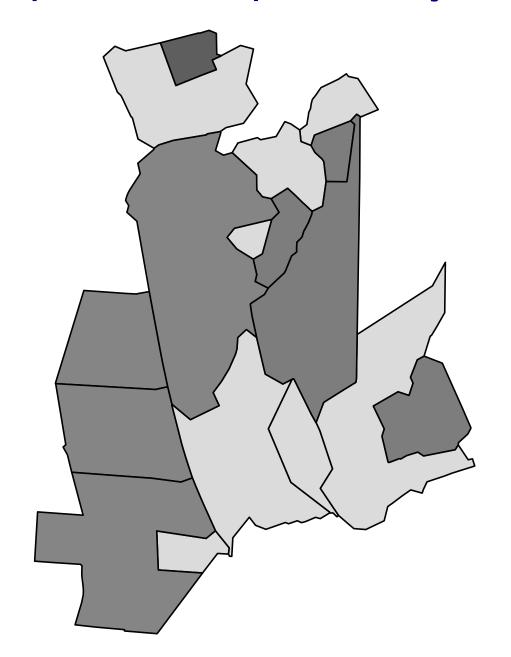
20-2

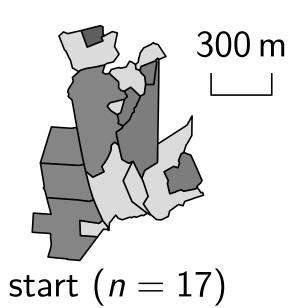
scale 1:250 k

Comparison of A* and ILP

percentage of regions that were found optimal solutions

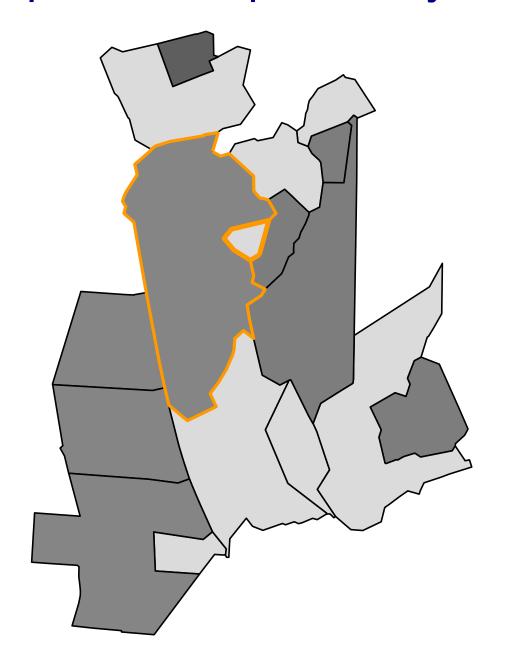


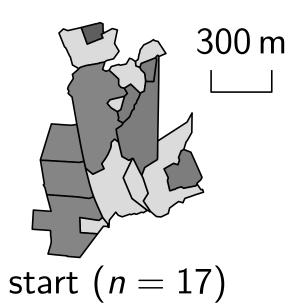




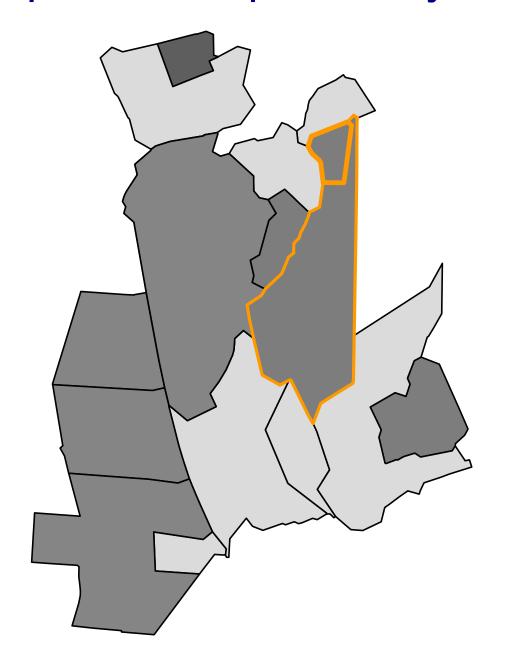


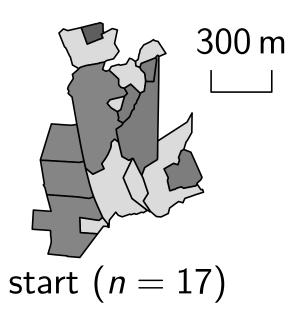
goal



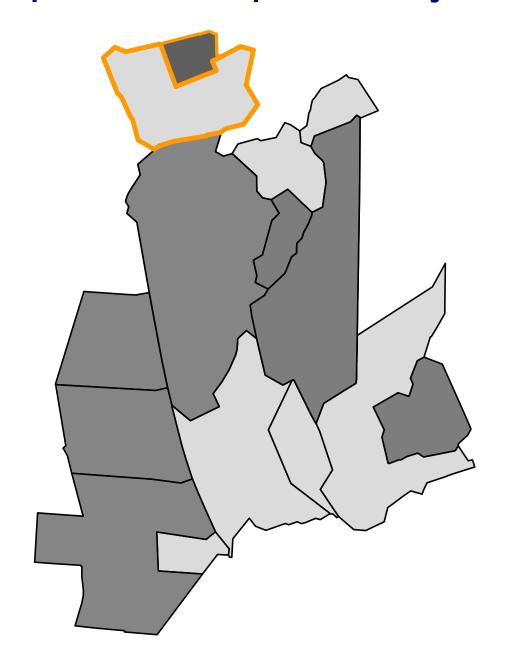


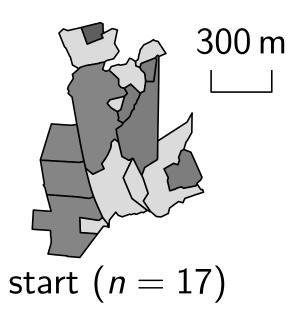




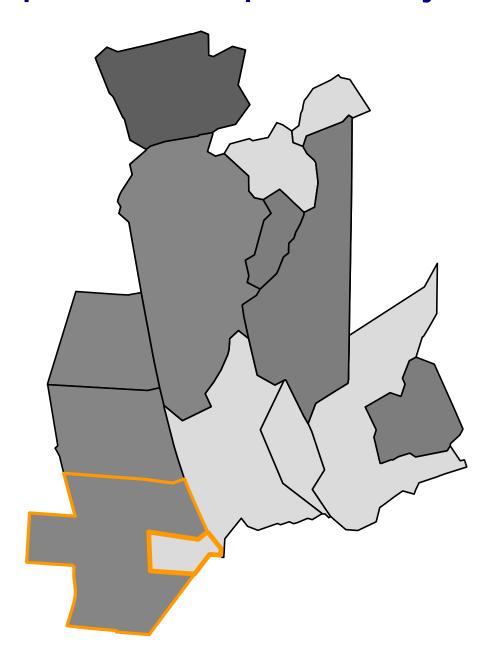


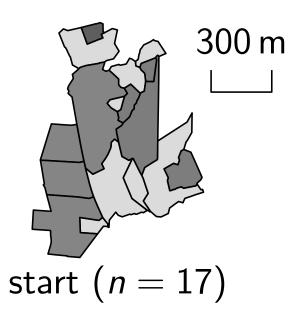




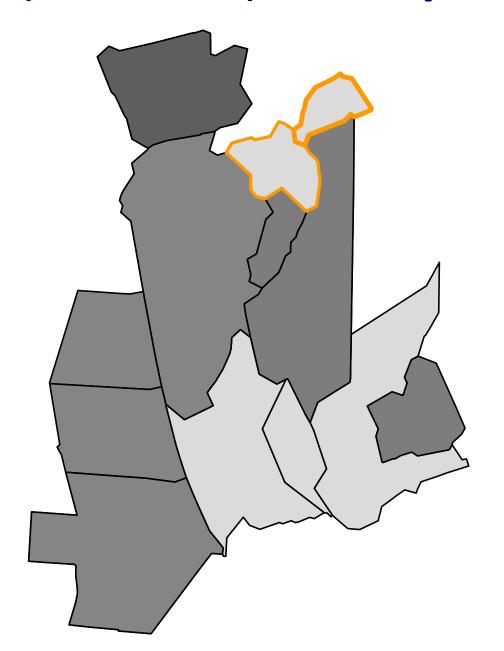


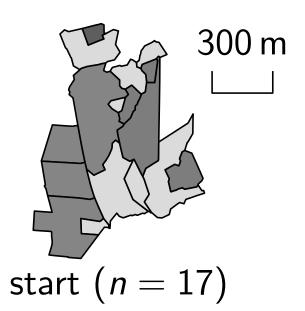




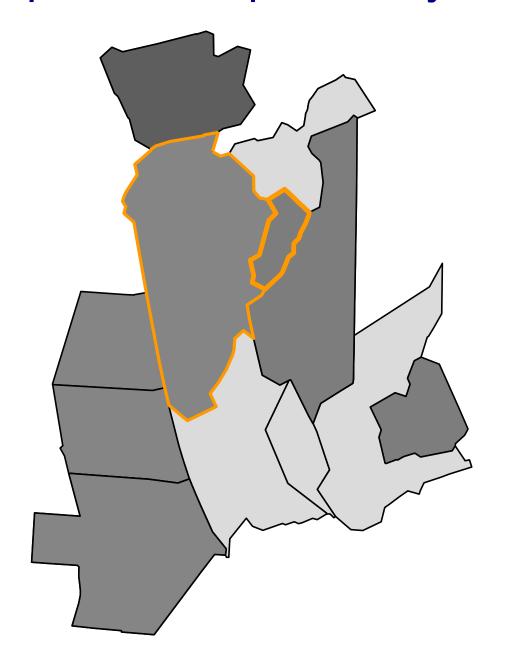


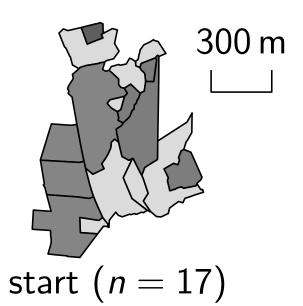




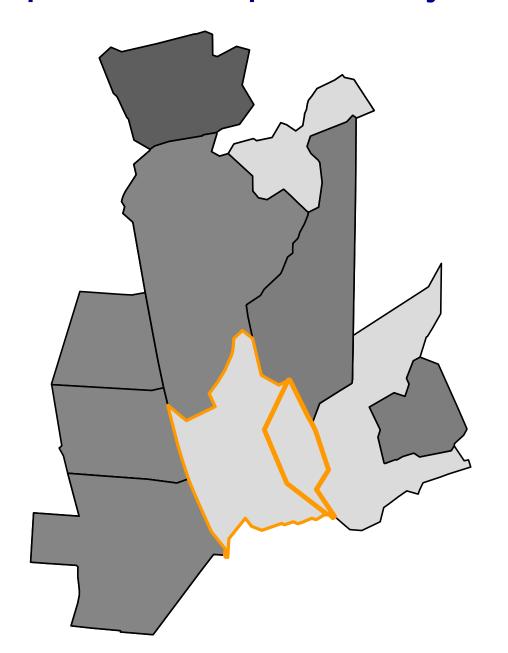


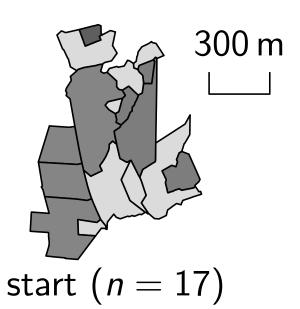




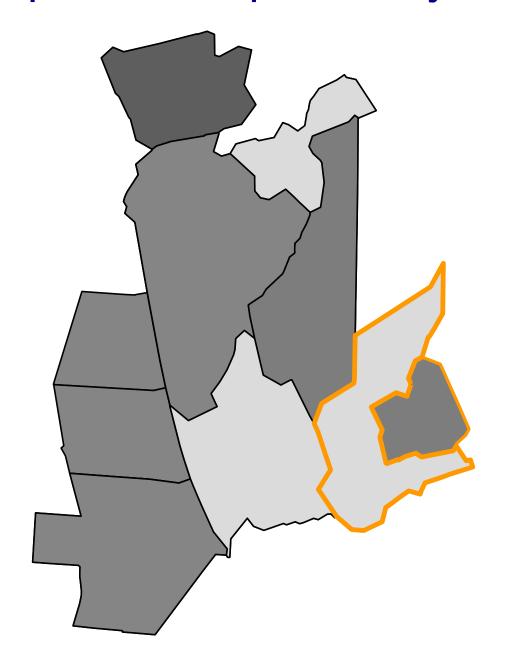


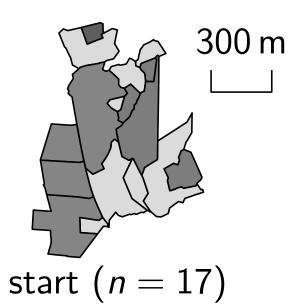




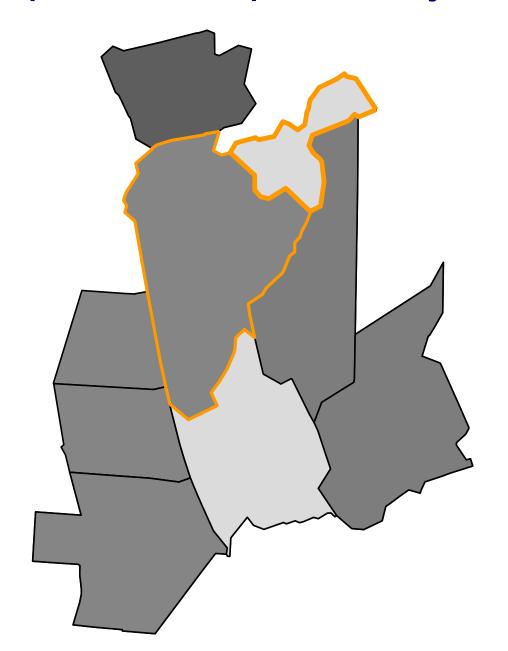


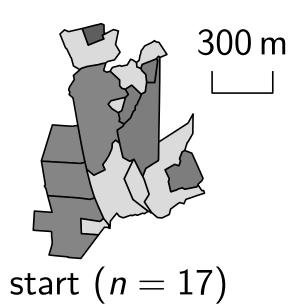




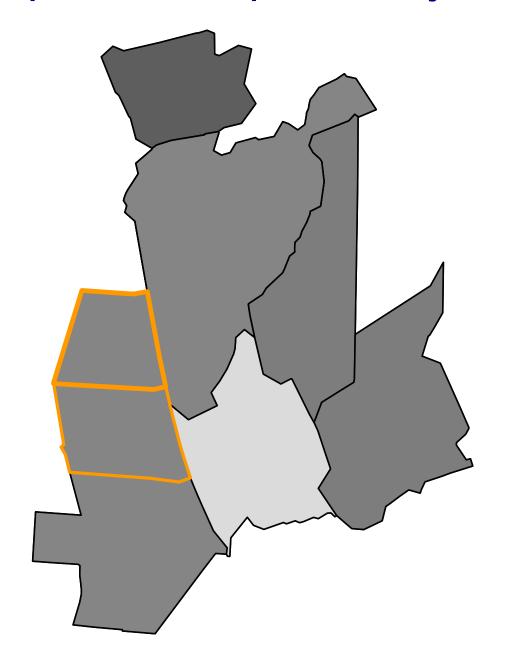


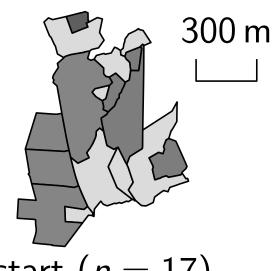


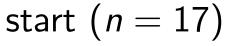




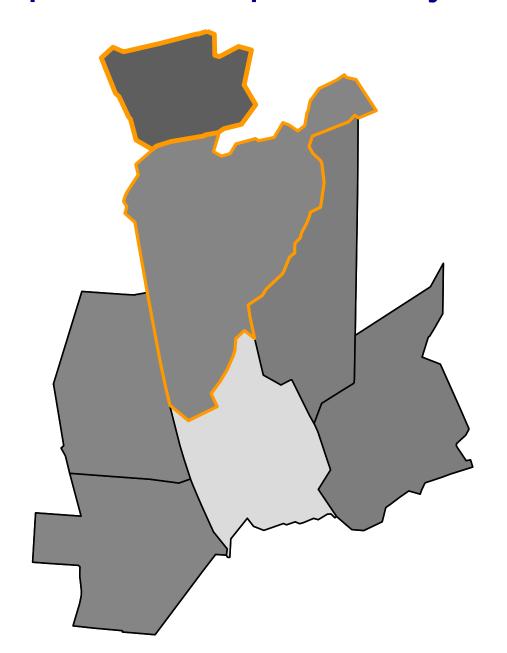


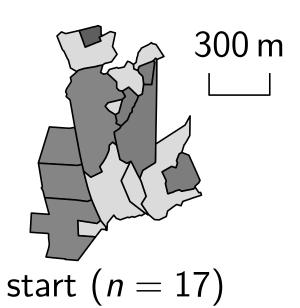




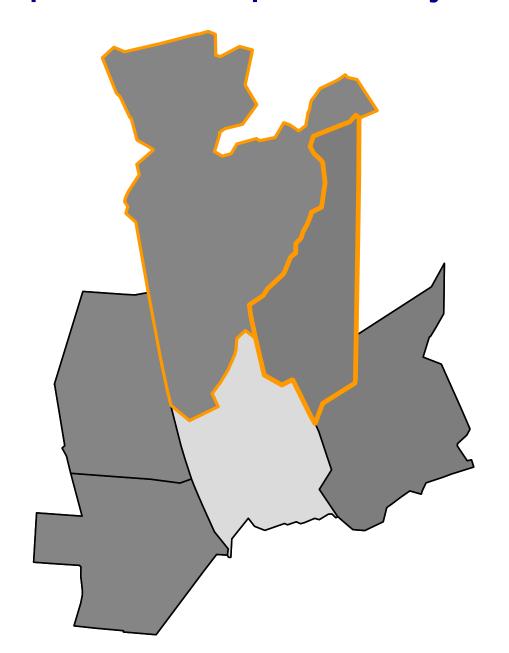


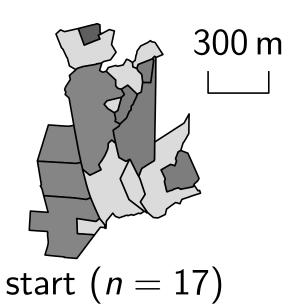




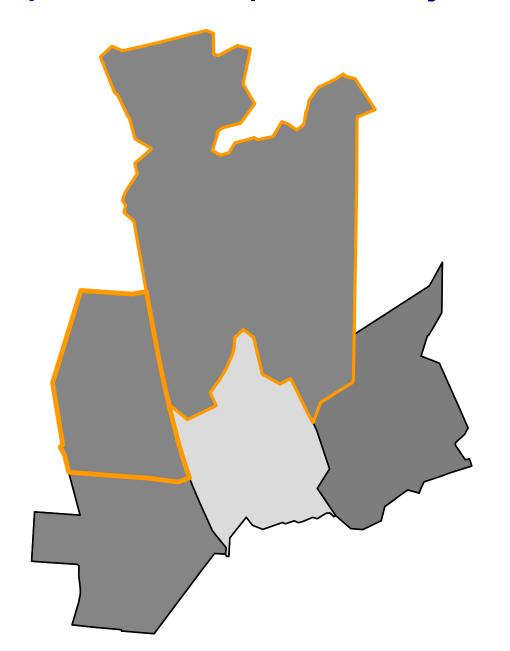


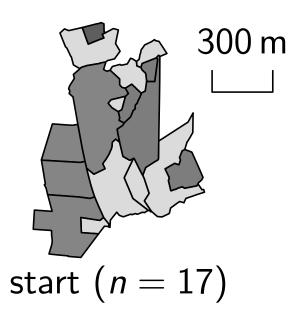




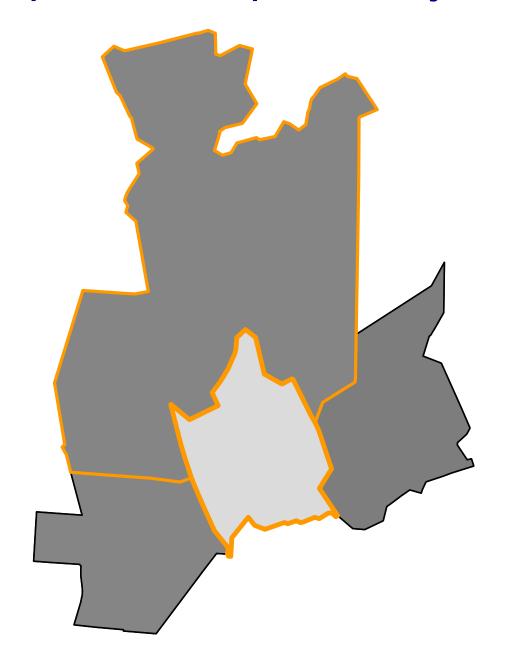


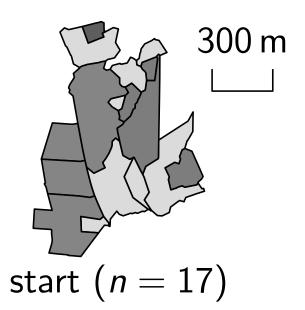


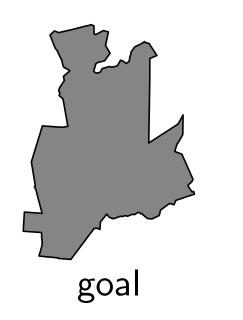


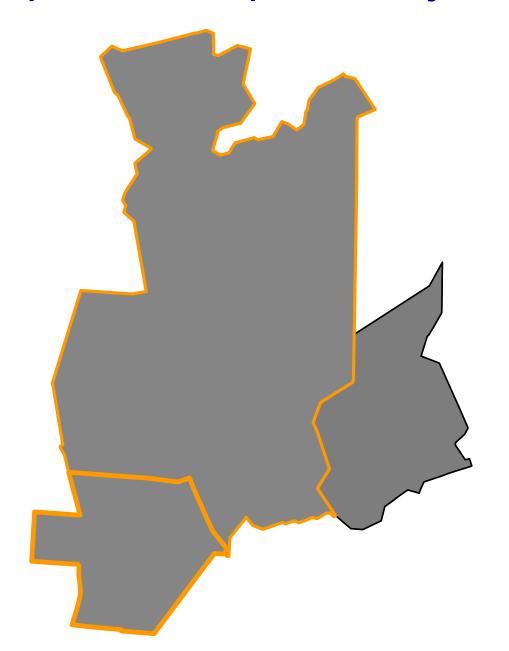


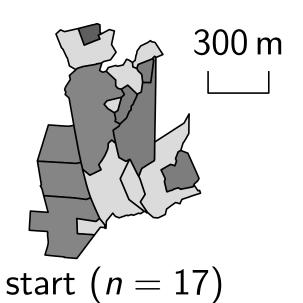




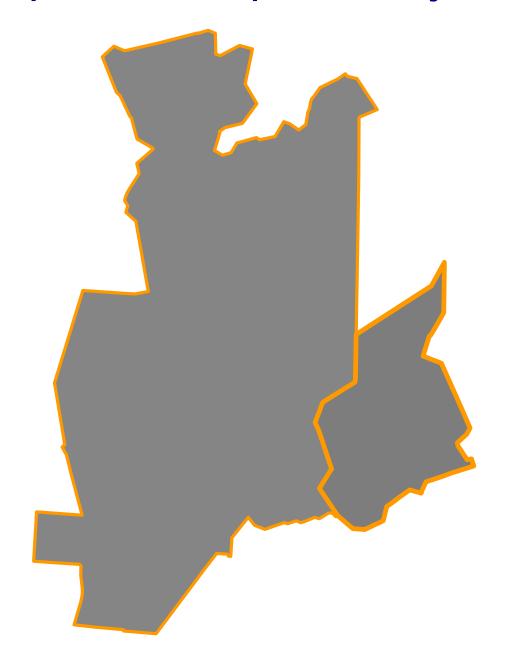


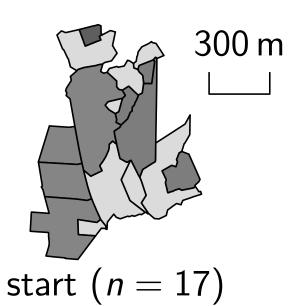






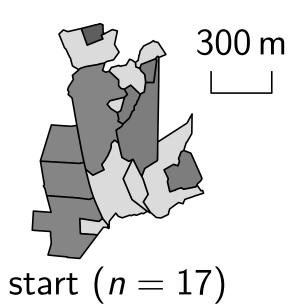












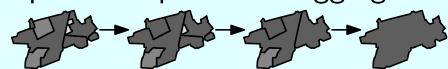


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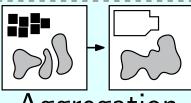
Optim.

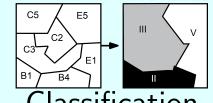
Related Generalization

Optimal sequence for aggregation



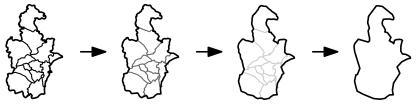
A* ILP



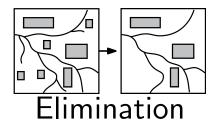


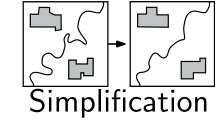
Aggregation Classification

Administrative boundaires

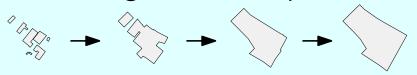


DP

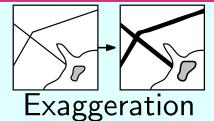




Buildings to built-up areas



MST

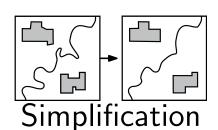


Aggregation, Simplification, Elimination

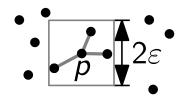
Morphing polylines



LSA DP

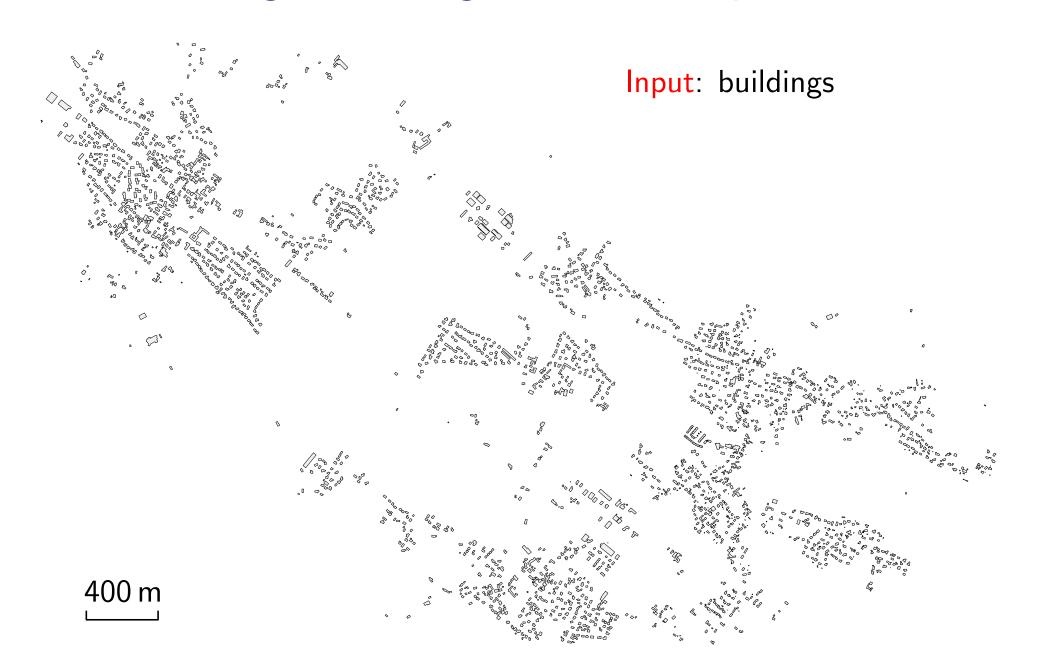


Choosing right data structures

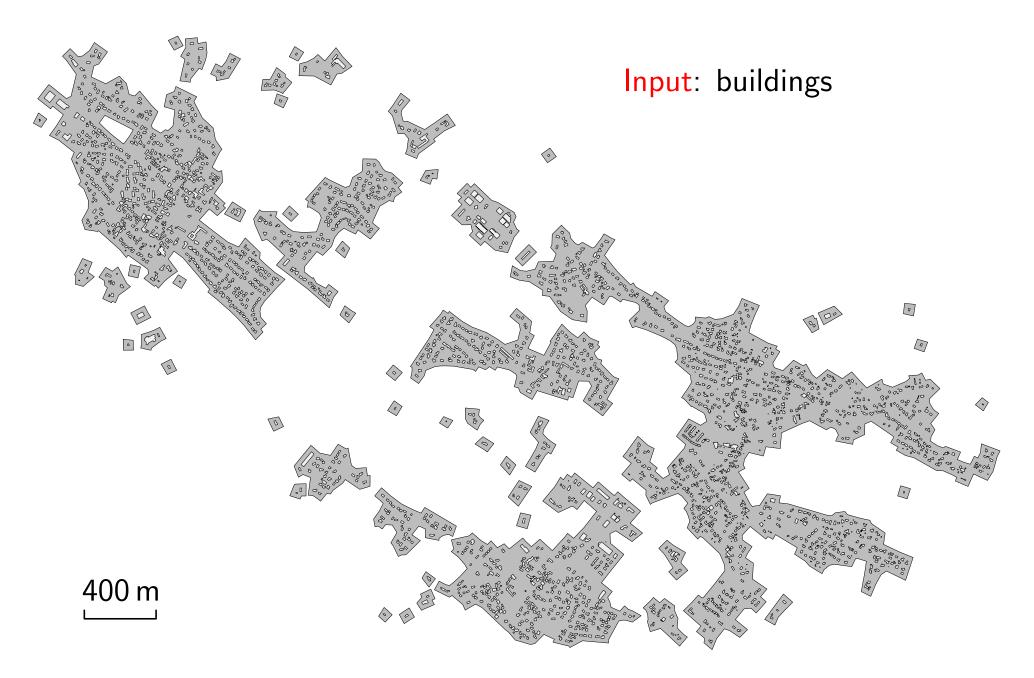


SortedDictionary, SortedSet, ...

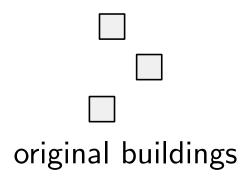
Generalizing Buildings to Built-up Areas



Generalizing Buildings to Built-up Areas



Aggregate buildings that are too close, when zooming out



- Aggregate buildings that are too close, when zooming out
- Bridges and buildings constitute a minimum spanning tree (MST)

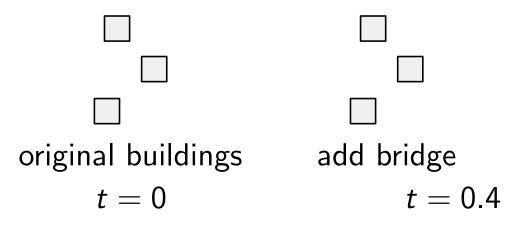
original buildings

- Aggregate buildings that are too close, when zooming out
- Bridges and buildings constitute a minimum spanning tree (MST)

 \Box \Box \Box original buildings t=0

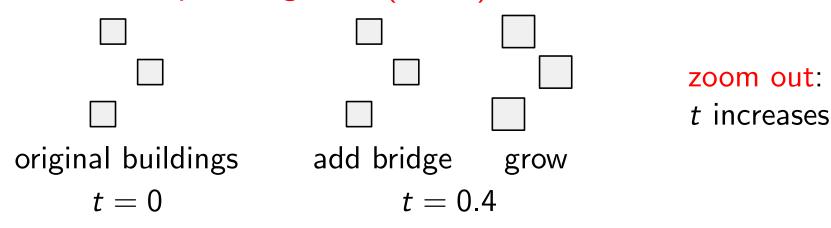
zoom out:

- Aggregate buildings that are too close, when zooming out
- Bridges and buildings constitute a minimum spanning tree (MST)

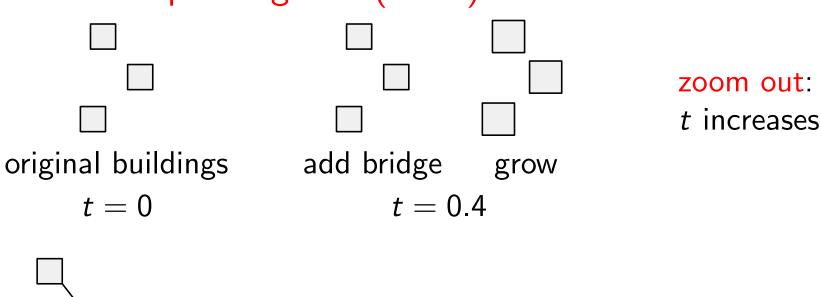


zoom out:

- Aggregate buildings that are too close, when zooming out
- Bridges and buildings constitute a minimum spanning tree (MST)

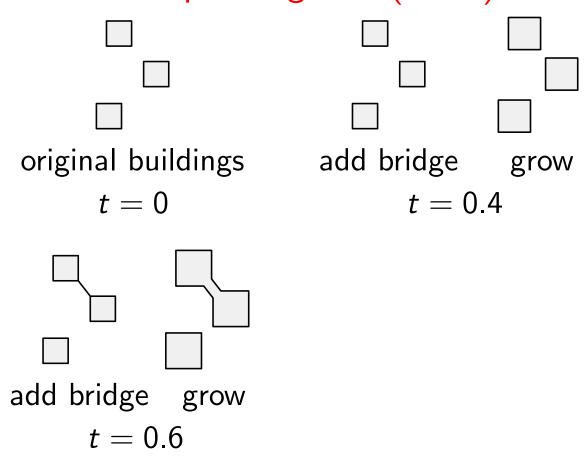


- Aggregate buildings that are too close, when zooming out
- Bridges and buildings constitute a minimum spanning tree (MST)



add bridge t = 0.6

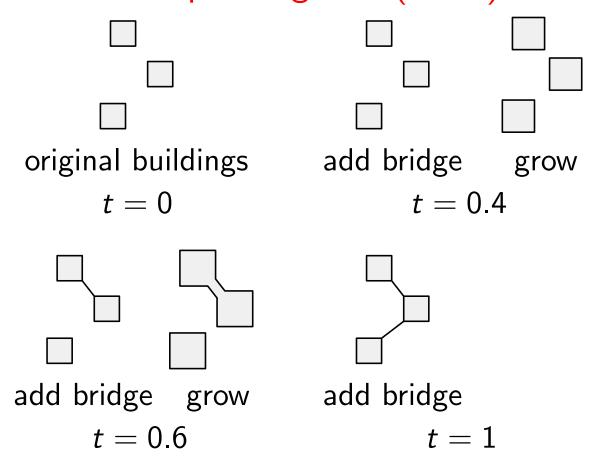
- Aggregate buildings that are too close, when zooming out
- Bridges and buildings constitute a minimum spanning tree (MST)



25-7

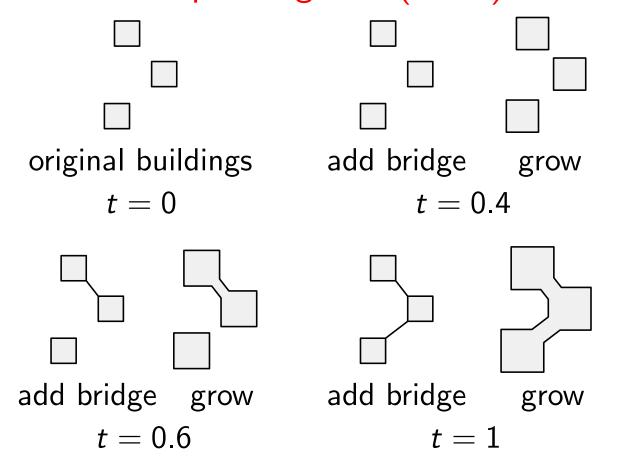
zoom out:

- Aggregate buildings that are too close, when zooming out
- Bridges and buildings constitute a minimum spanning tree (MST)

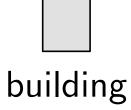


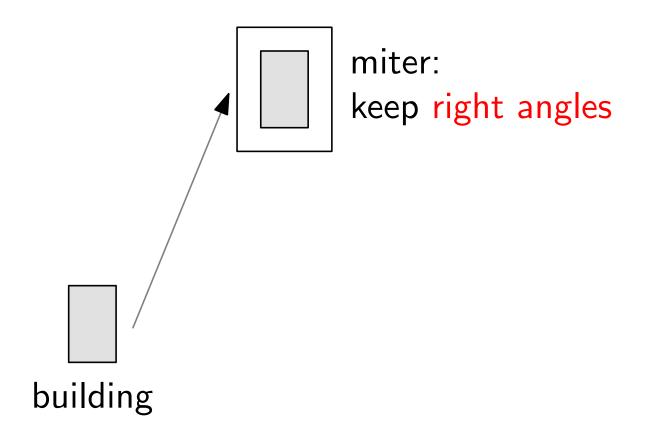
zoom out:

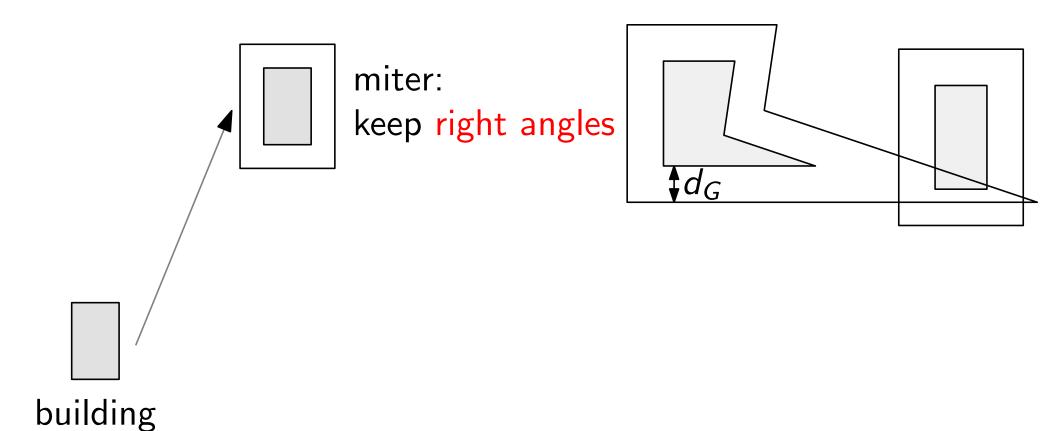
- Aggregate buildings that are too close, when zooming out
- Bridges and buildings constitute a minimum spanning tree (MST)

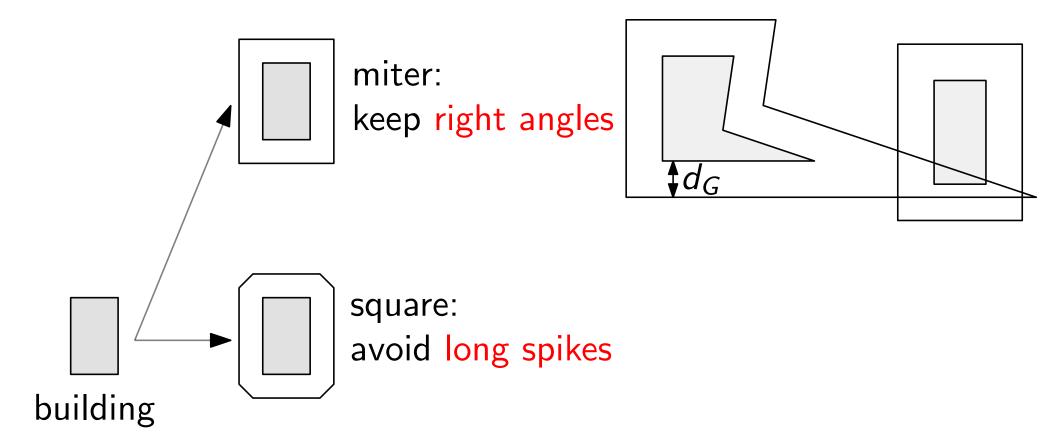


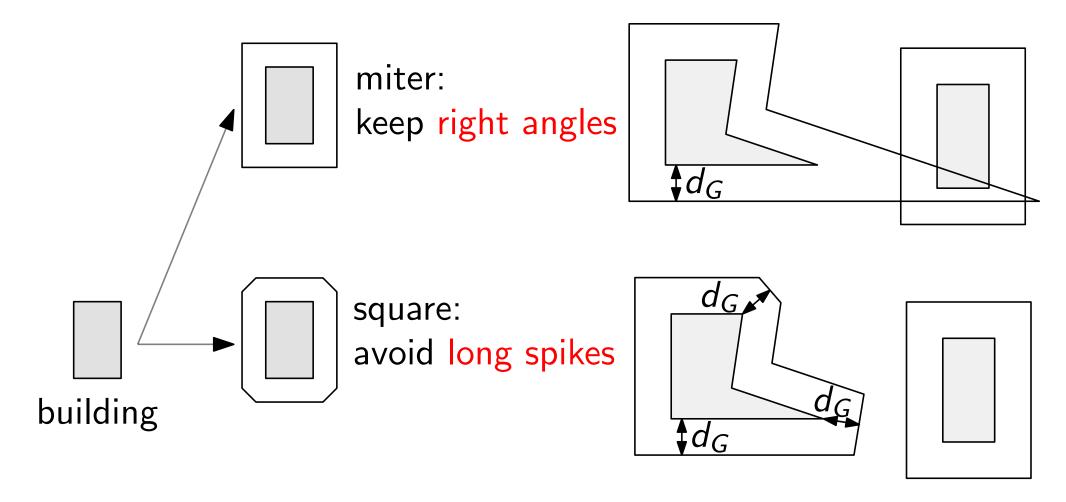
zoom out:

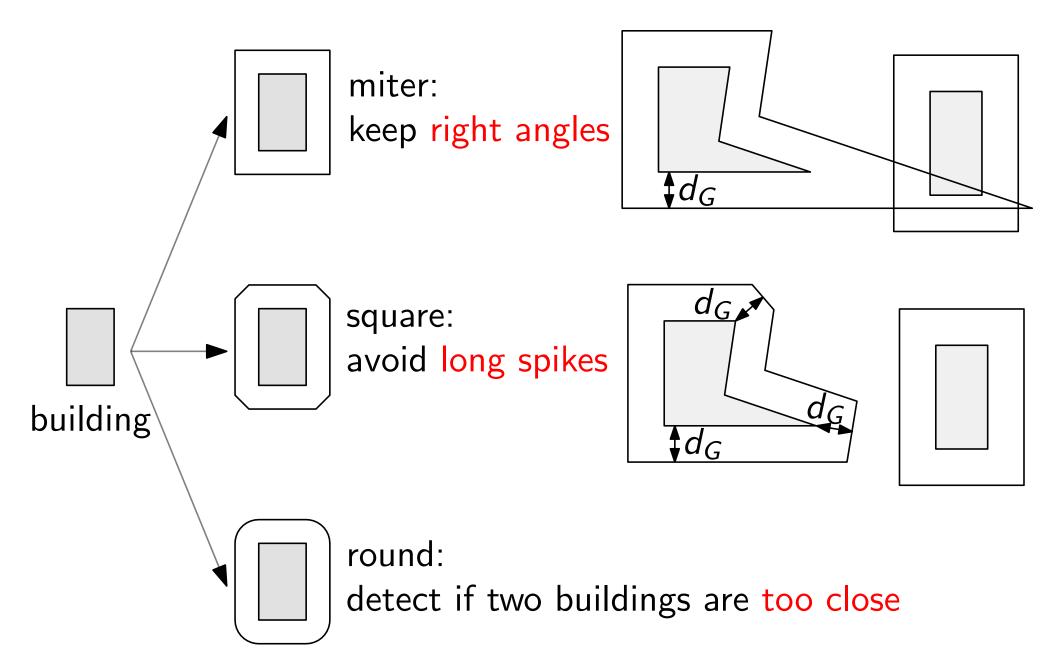


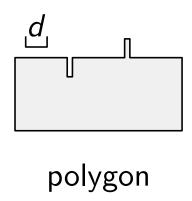


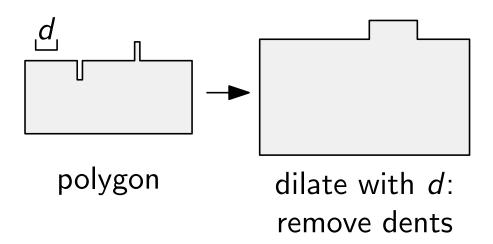


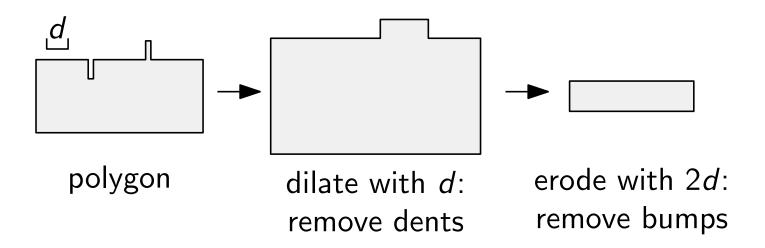


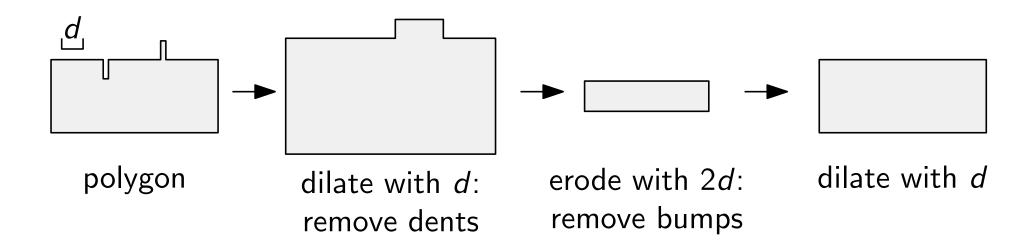












• Runtime: $O(n^3)$, n: total number of edges over all input buildings

- Runtime: $O(n^3)$, n: total number of edges over all input buildings
- Environment
 C#, CLIPPER (for buffering, dilation, erosion, and merge)

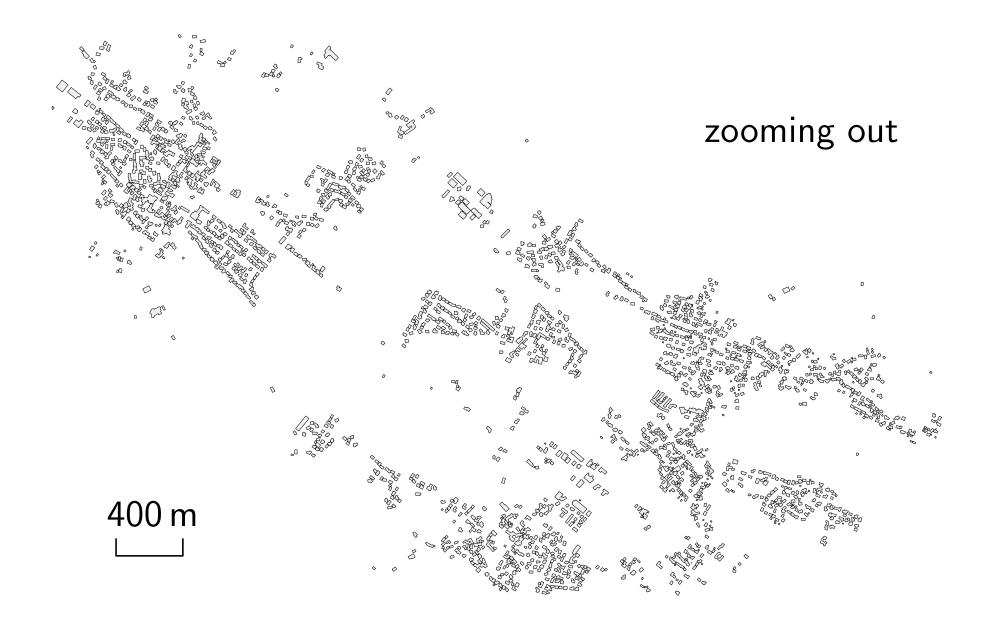
- Runtime: $O(n^3)$, n: total number of edges over all input buildings
- Environment
 C#, CLIPPER (for buffering, dilation, erosion, and merge)
- Data: 2.5 k buildings, n = 19 k edges, 1 : 15 k, $d_G = 25$ m (IGN)

- Runtime: $O(n^3)$, n: total number of edges over all input buildings
- Environment
 C#, CLIPPER (for buffering, dilation, erosion, and merge)
- Data: 2.5 k buildings, n = 19 k edges, 1 : 15 k, $d_G = 25$ m (IGN)
- 12 min for computing a sequence of 10 maps

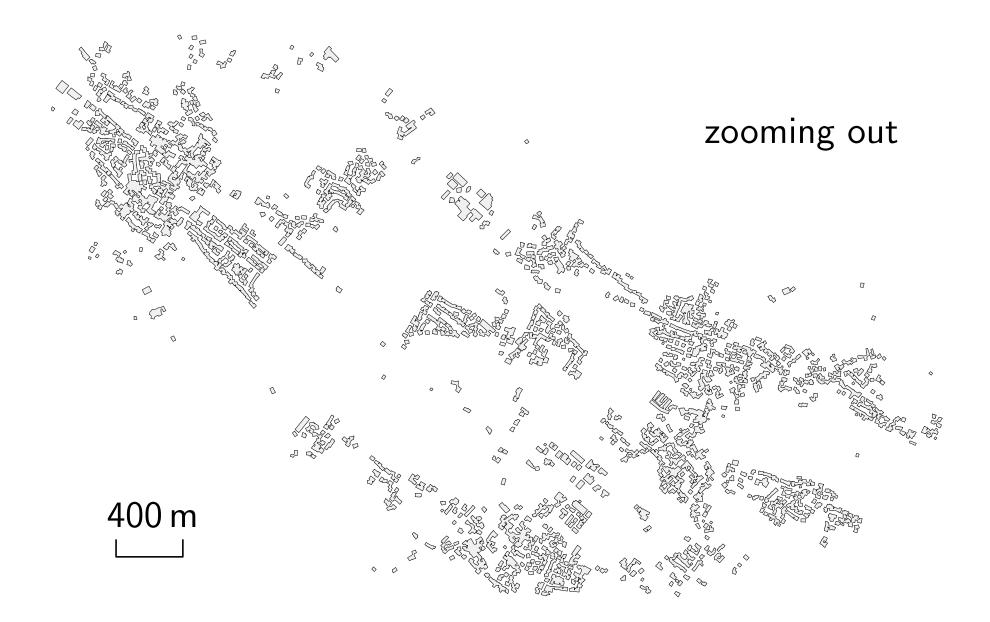
Animation

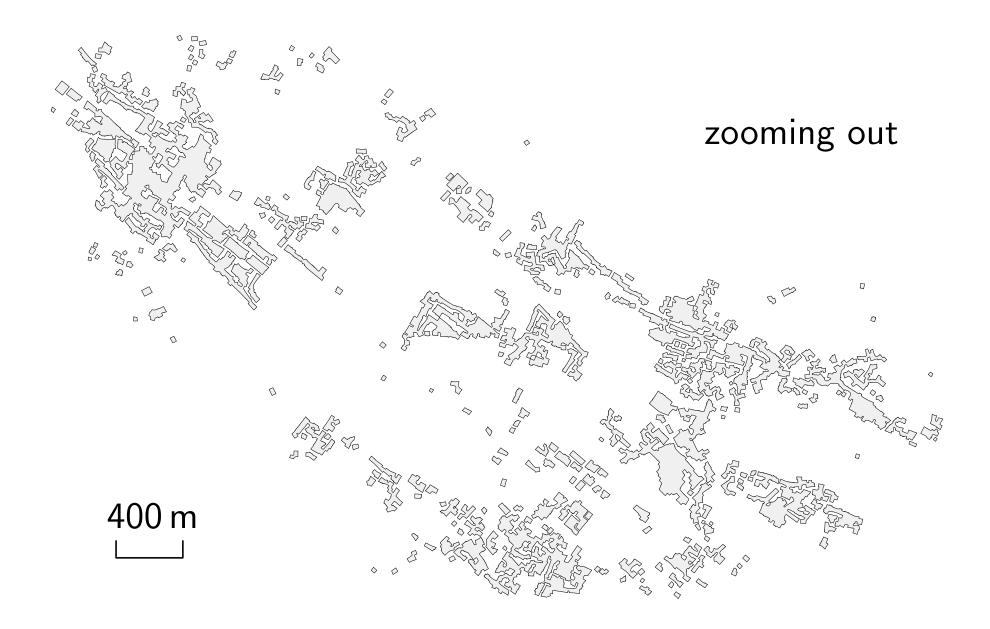


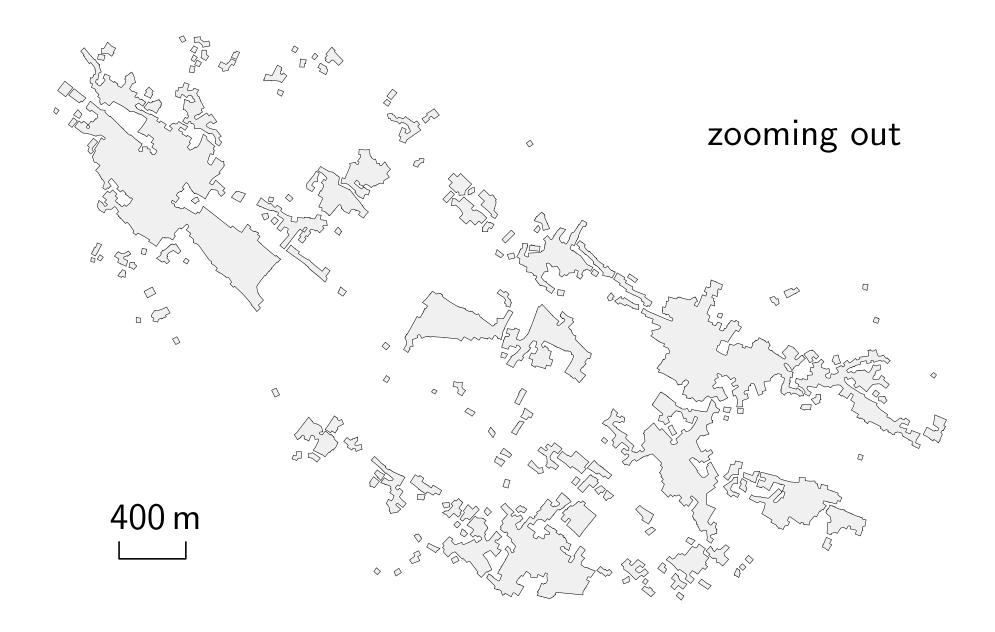
Animation



Animation

















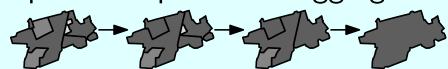


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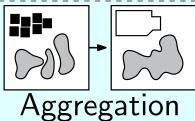
Optim.

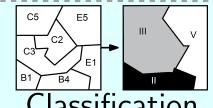
Related Generalization

Optimal sequence for aggregation



A* ILP



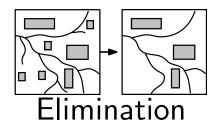


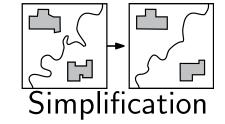
tion Classification

Administrative boundaires

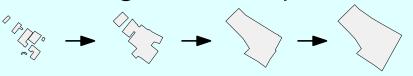


DP

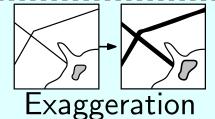




Buildings to built-up areas



MST

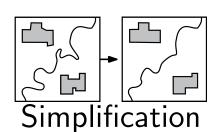


Aggregation, Simplification, Elimination

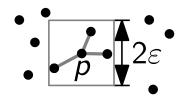
Morphing polylines



LSA DP



Choosing right data structures



SortedDictionary, SortedSet, ...

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Future work

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